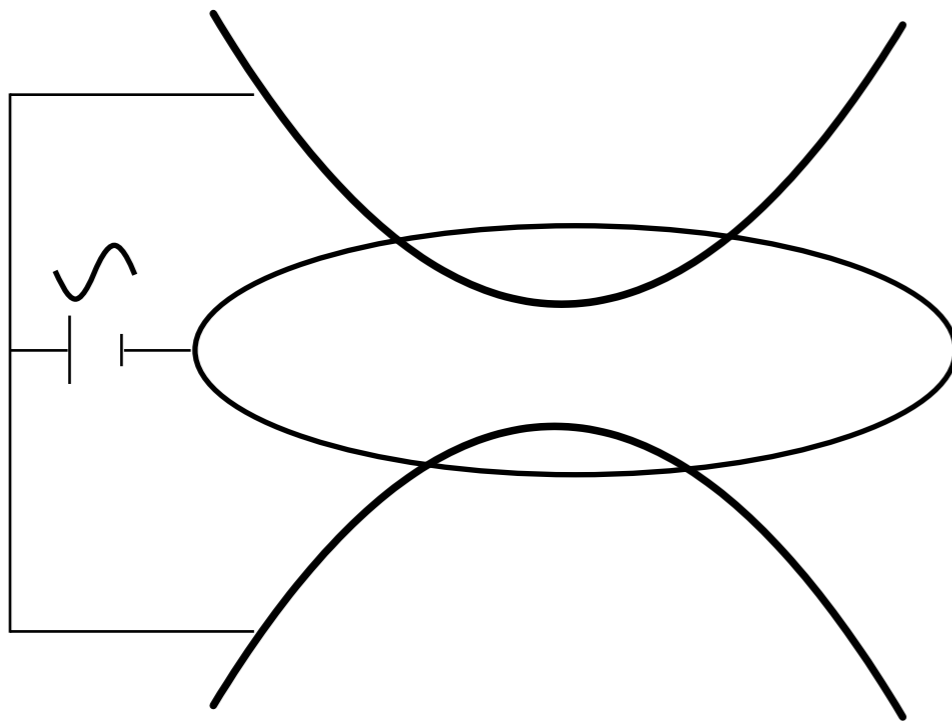
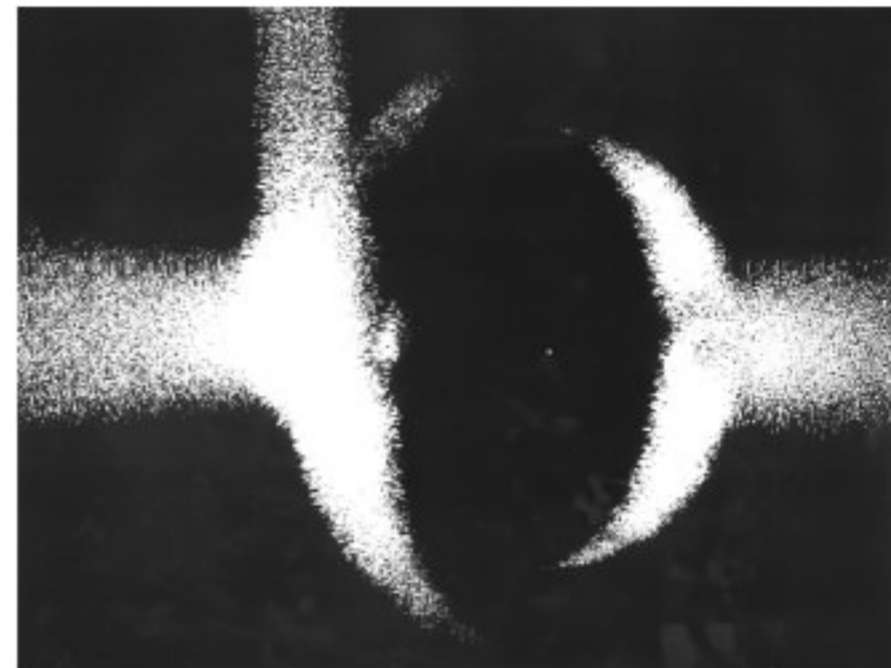
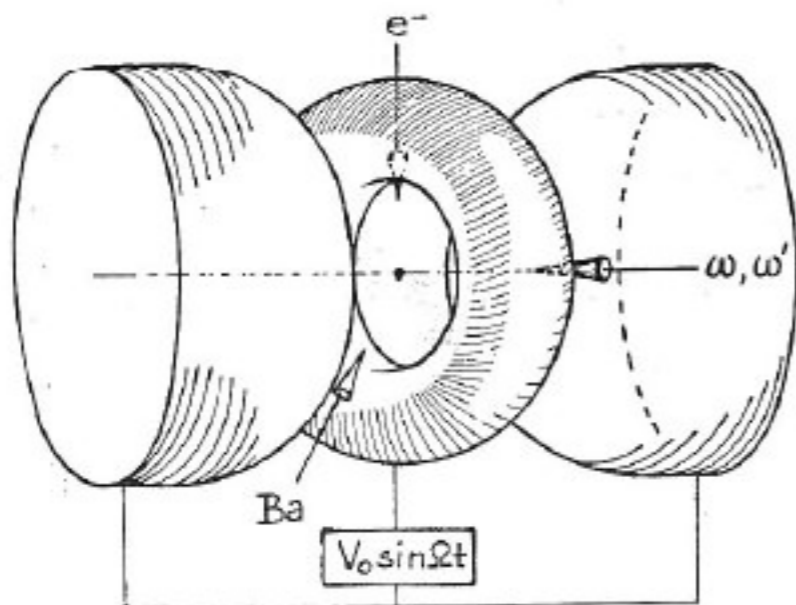
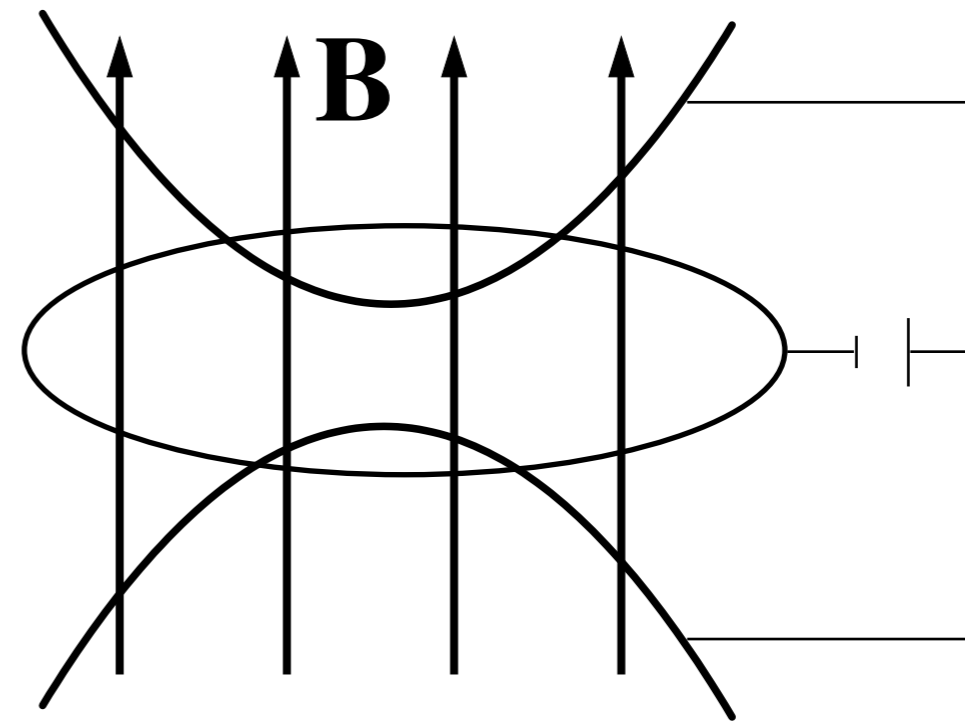


Ion Traps

Paul trap

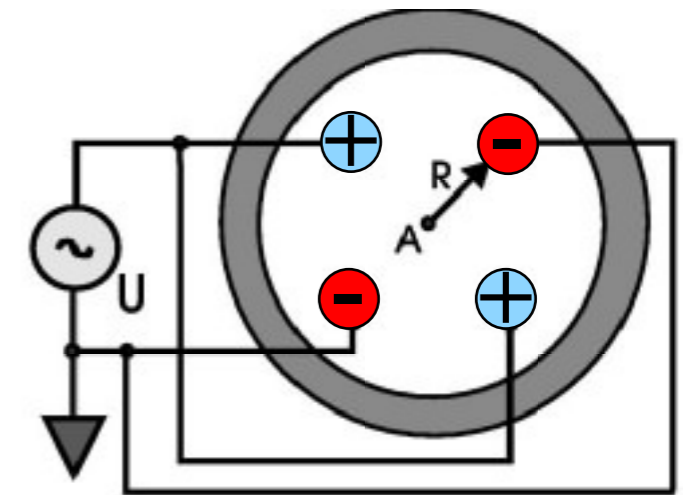
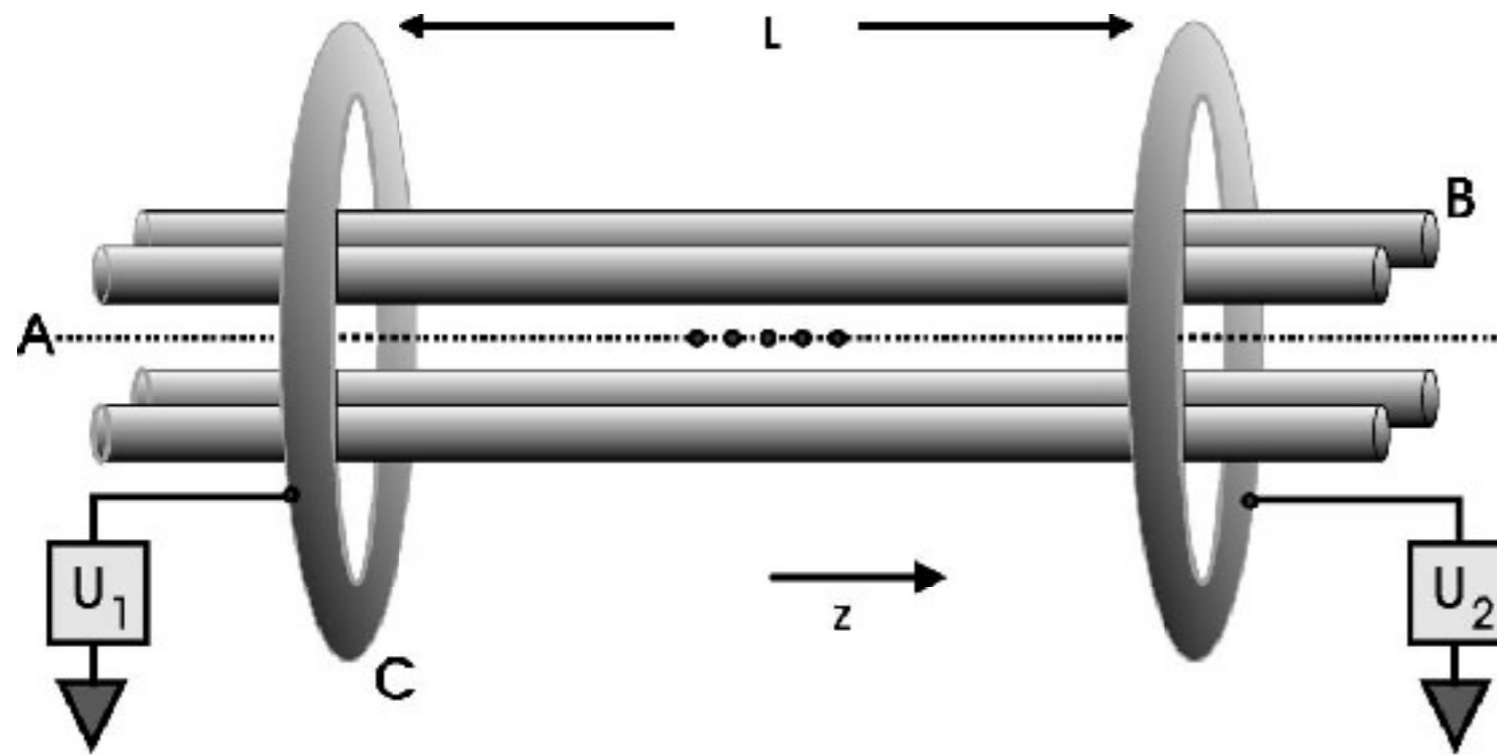


Penning trap



W. Neuhauser, M. Hohenstatt, P. E. Toschek,
H.G. Dehmelt, Phys. Rev. A 22, 1137 (1980).

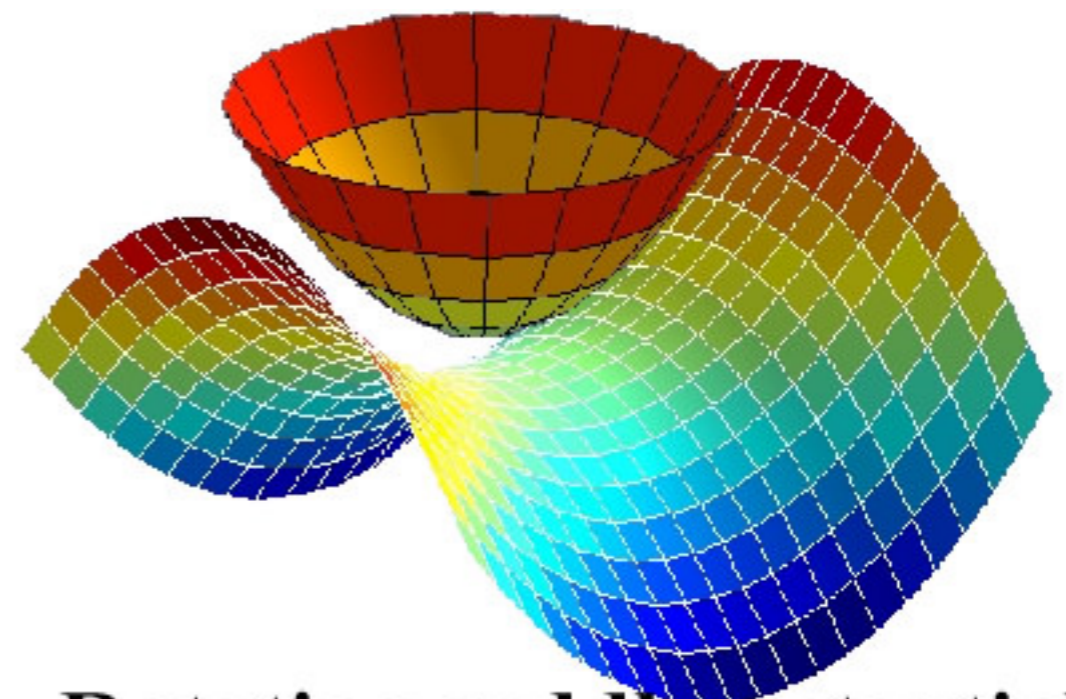
Linear Traps



Quadrupole field

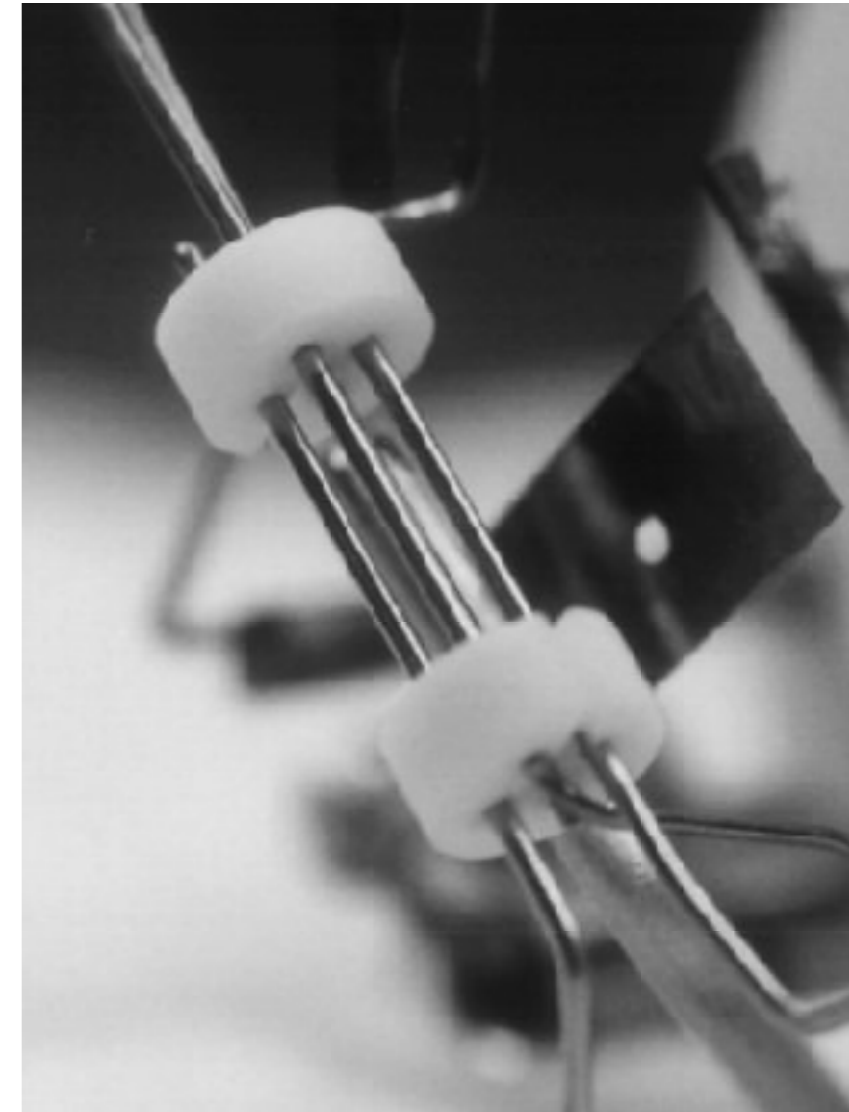
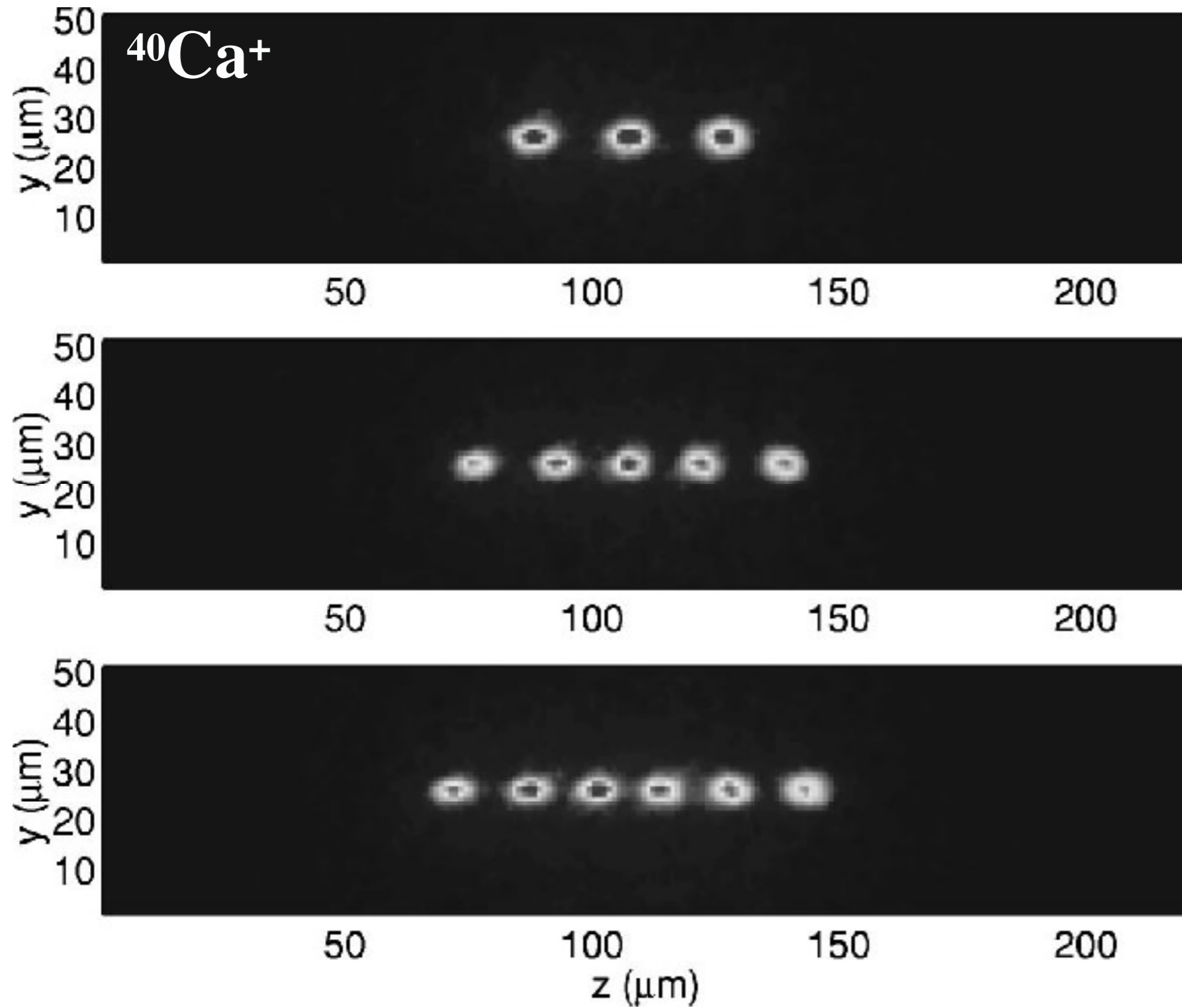
$$\Phi(x, y, t) = (U - V \cos \omega t) \frac{x^2 - y^2}{2r_0^2}$$

Time average



Rotating saddle potential

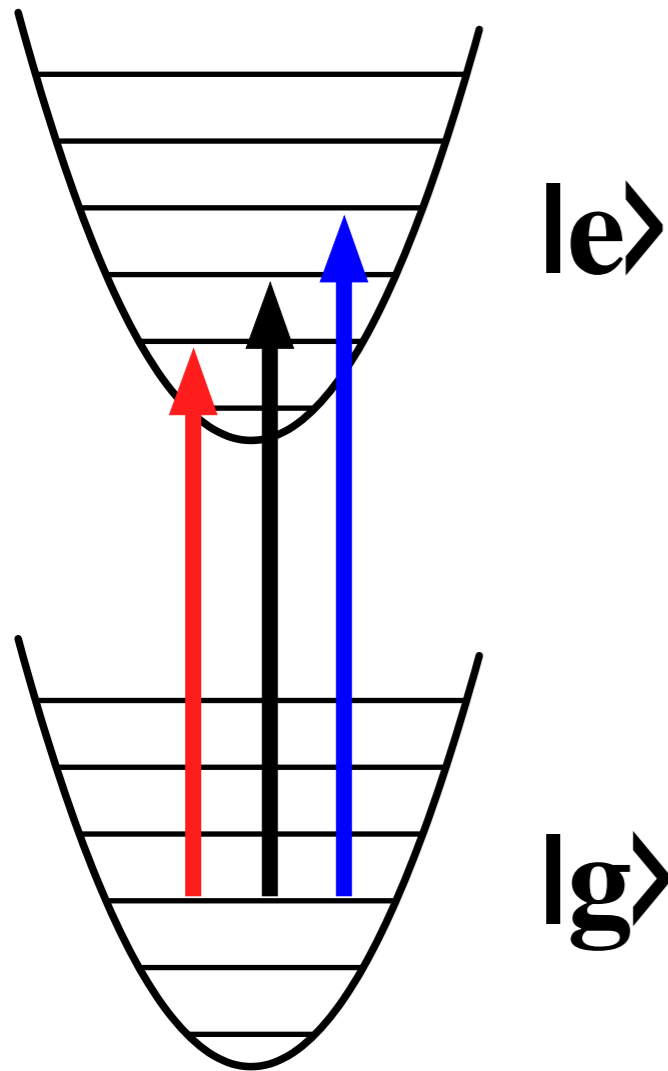
Trapped Ions



Motional States

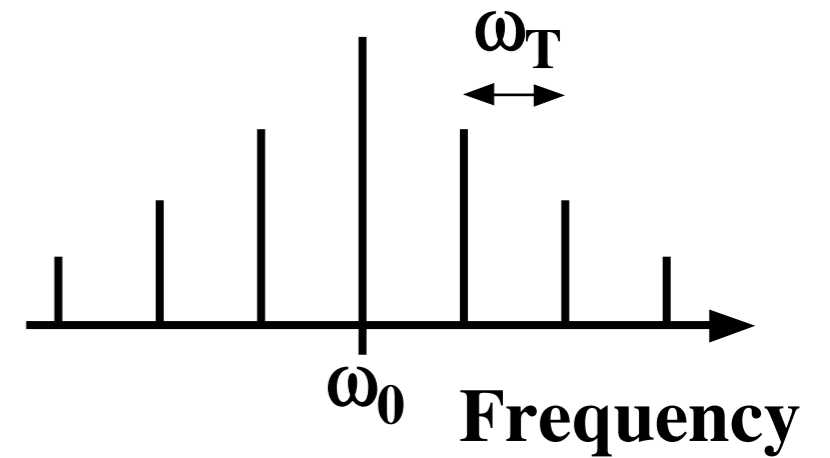
Confinement potential

$$V(\vec{r}) = \omega_x^2 x^2 + \omega_y^2 y^2 + \omega_z^2 z^2$$

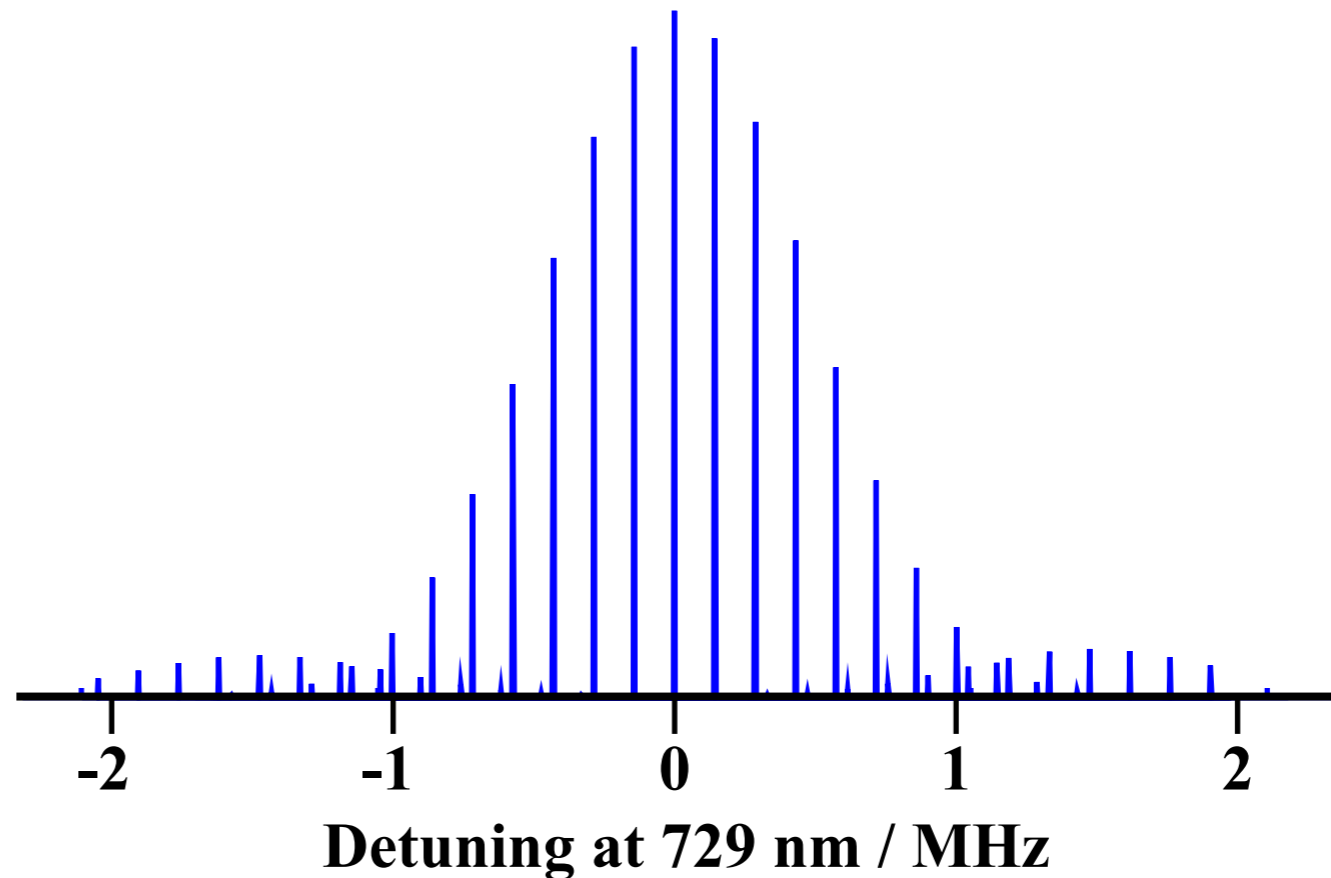


Single mode

carrier

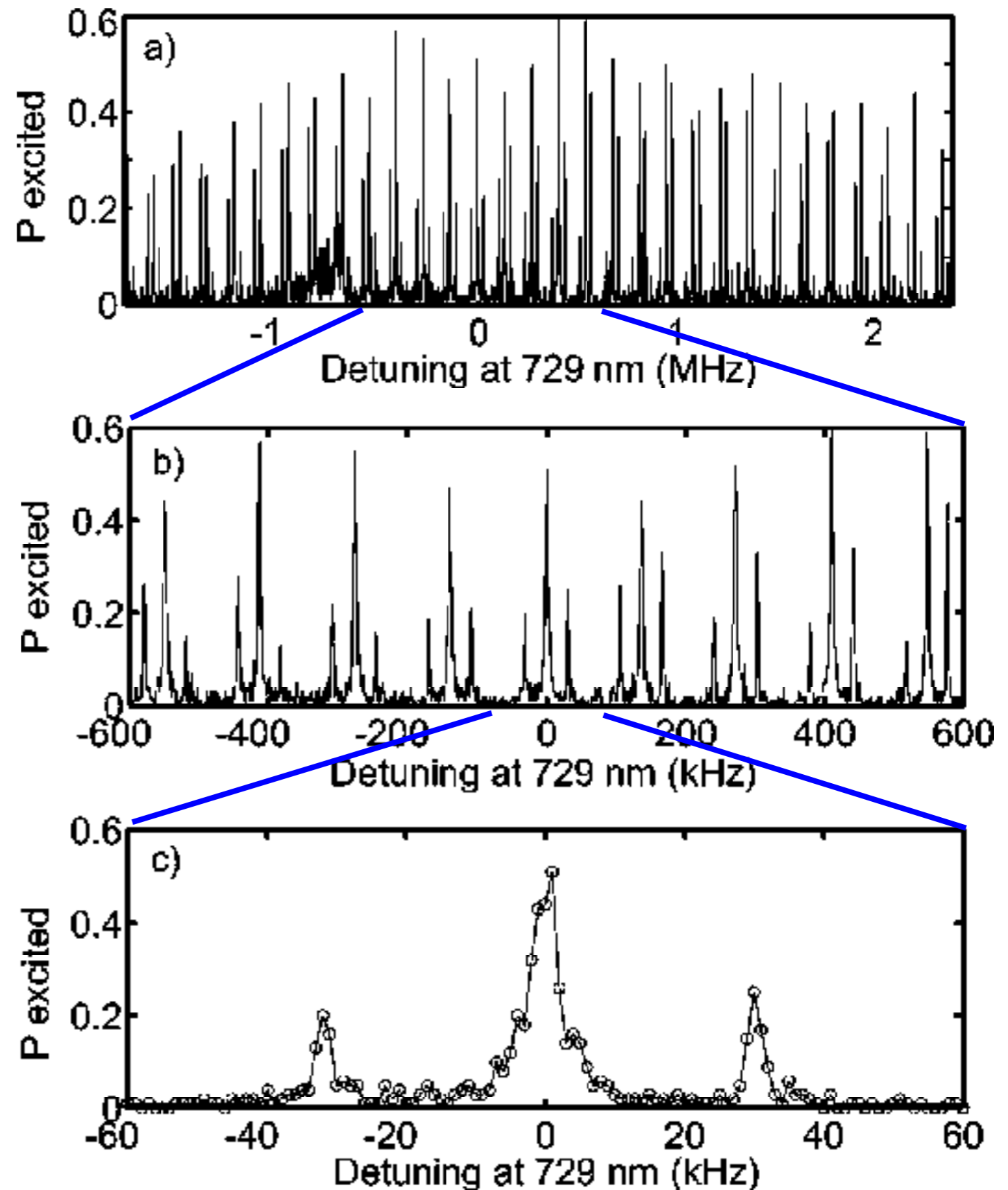


3 D

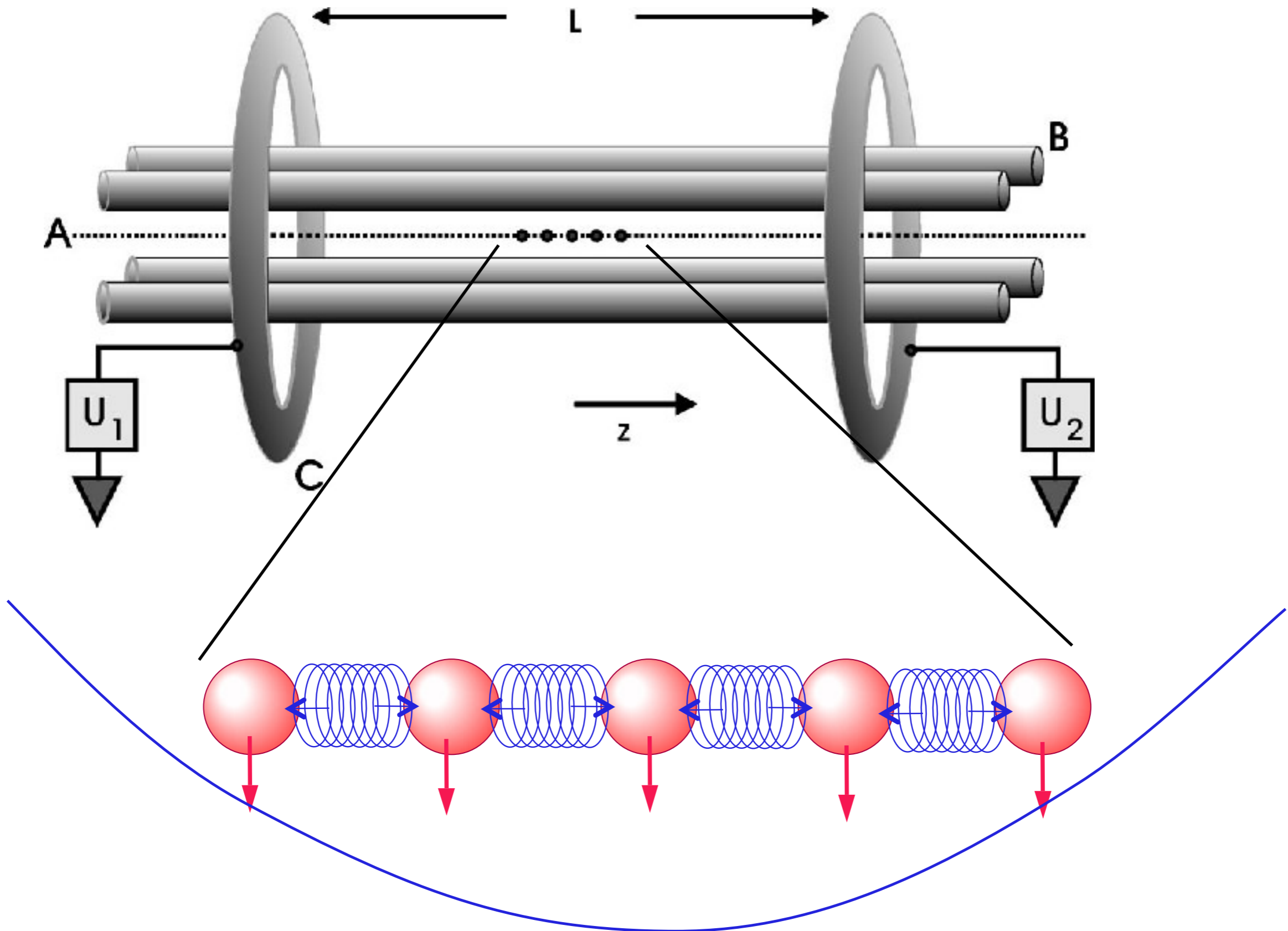


Sideband Spectrum

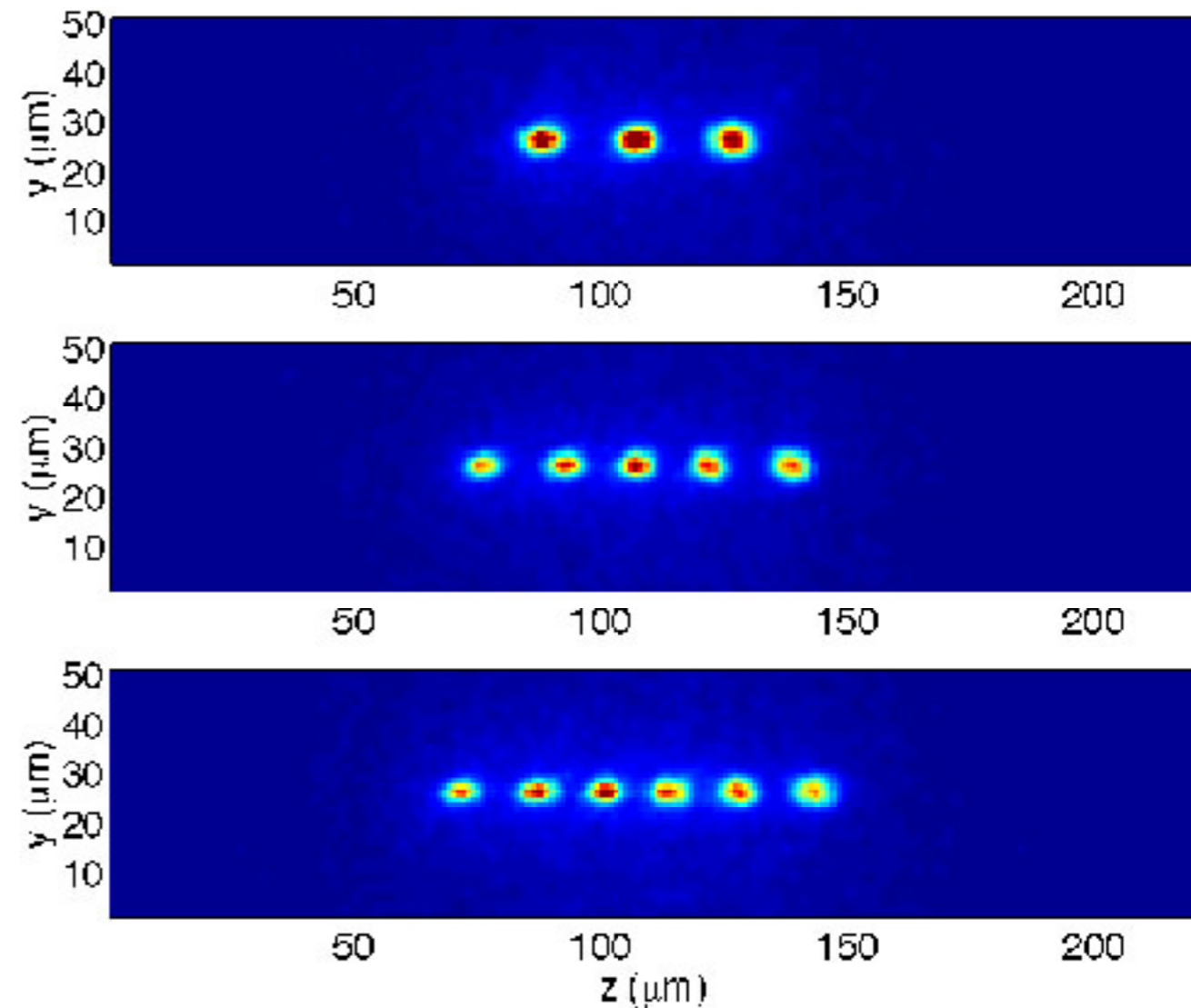
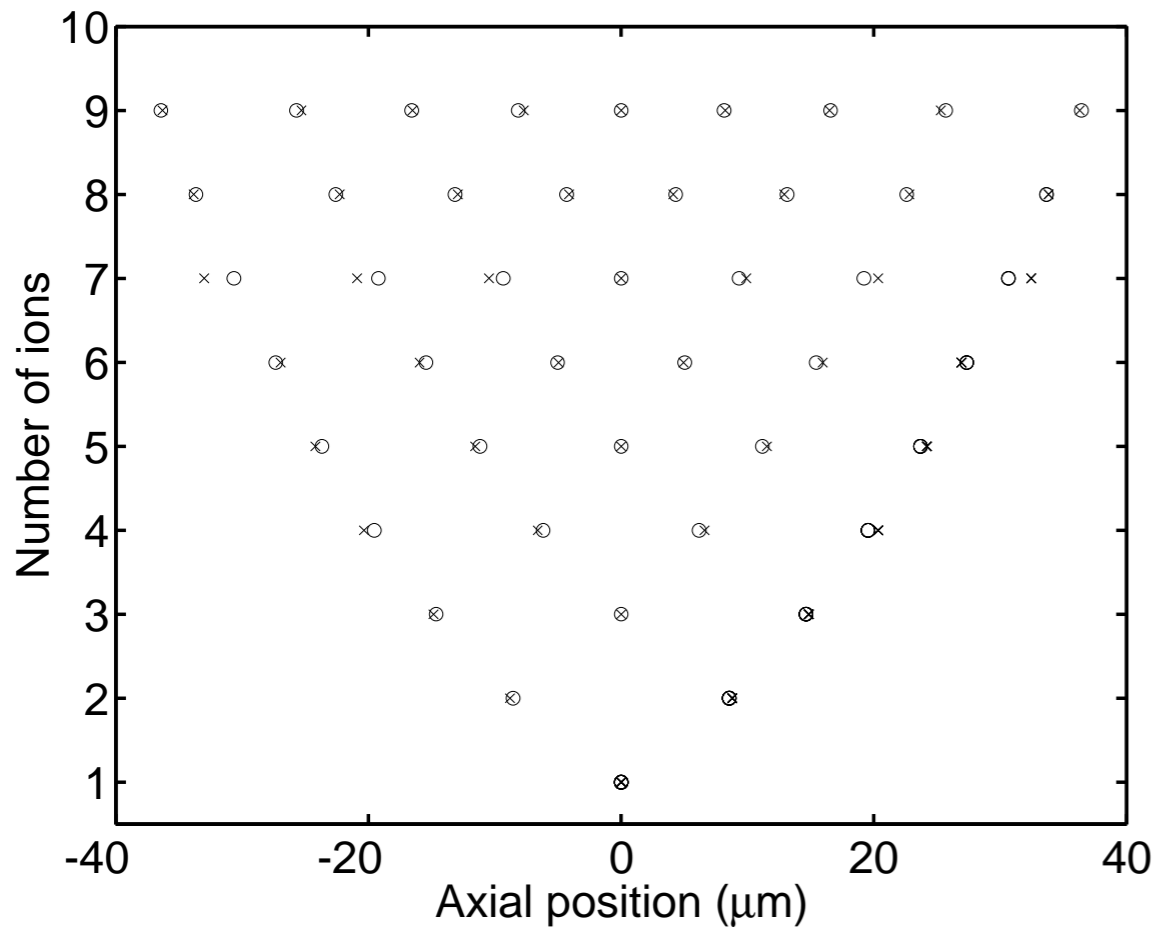
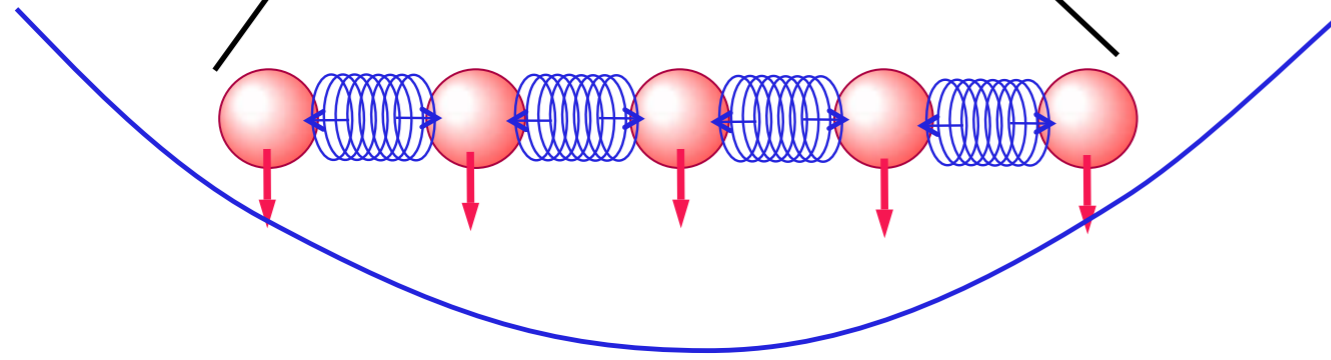
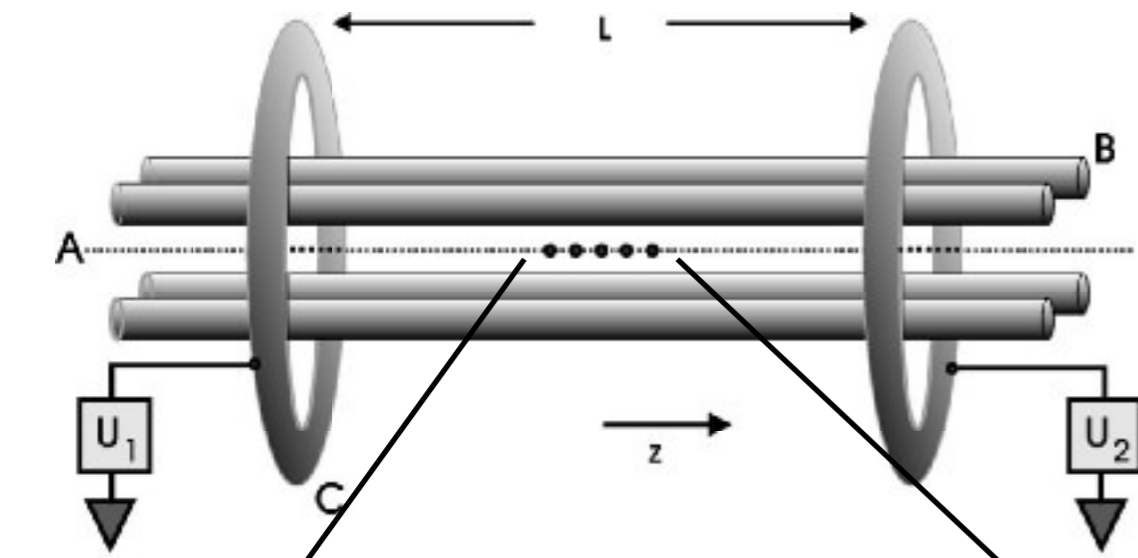
Ca^+



Multiple Ions

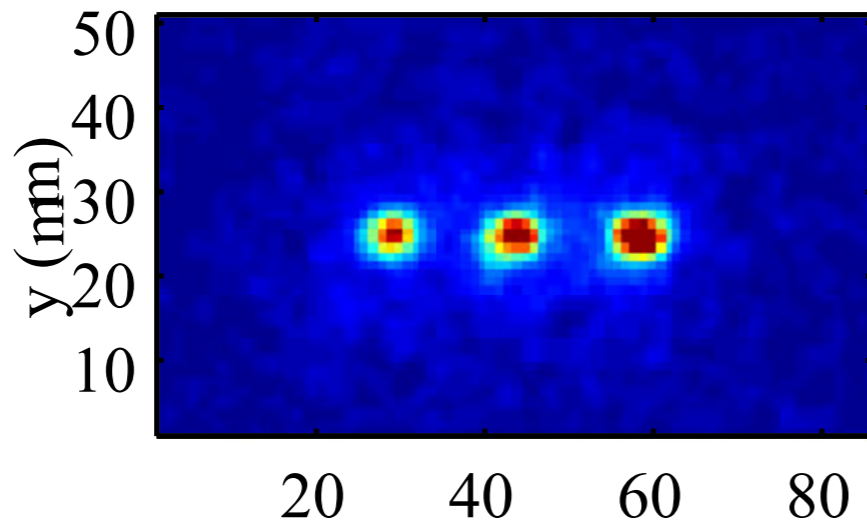


Multiple Ions

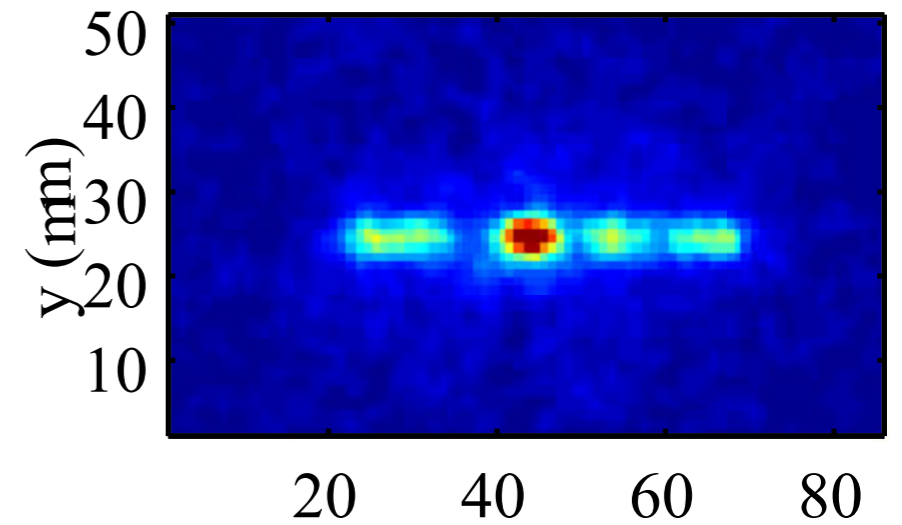


Collective Excitations

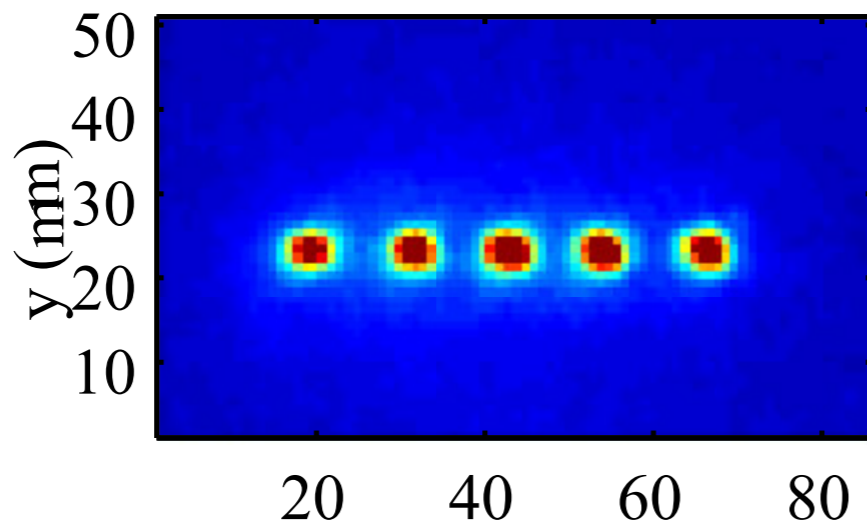
**3 ions
cold**



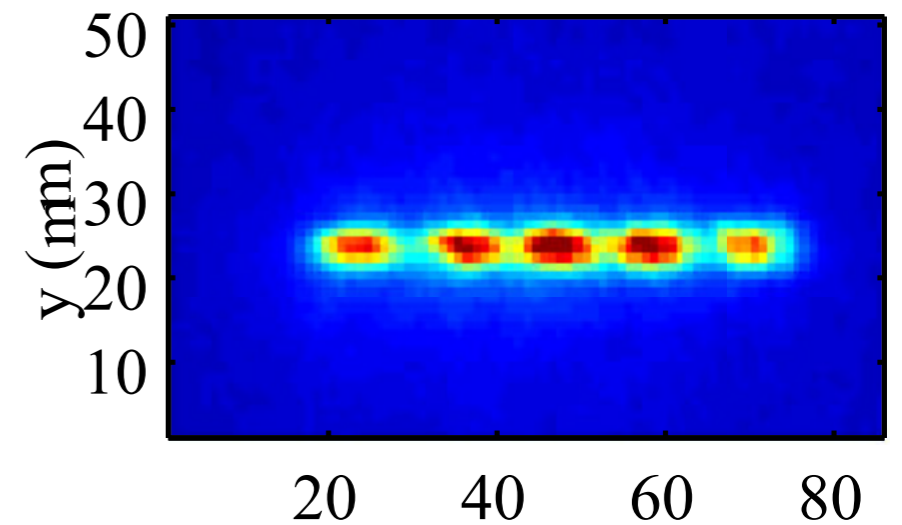
**3 ions
warm**



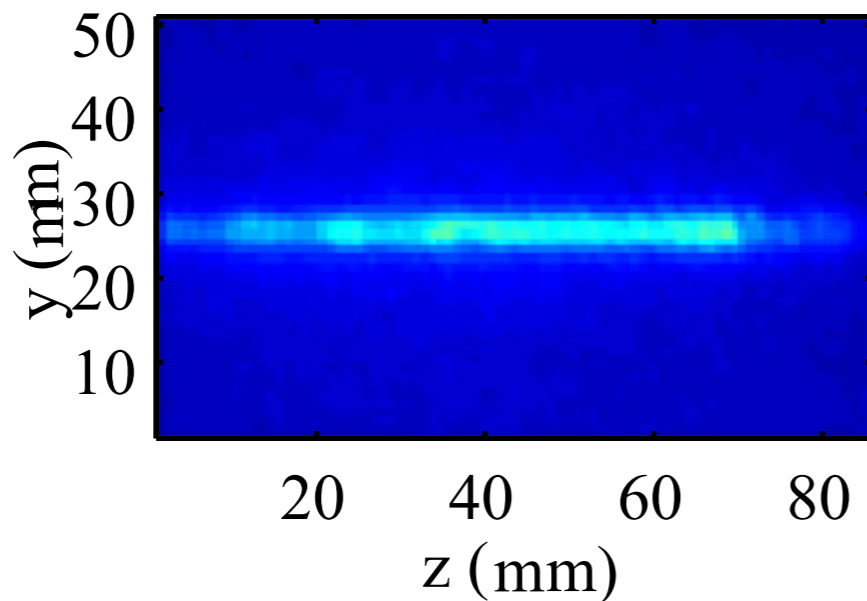
**5 ions
cold**



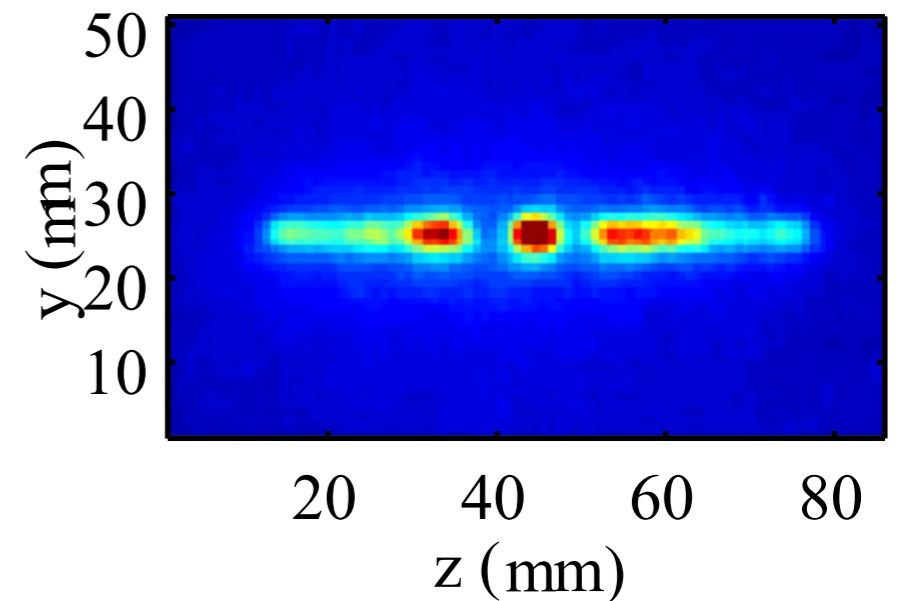
**5 ions
warm**



**5 ions
very hot**

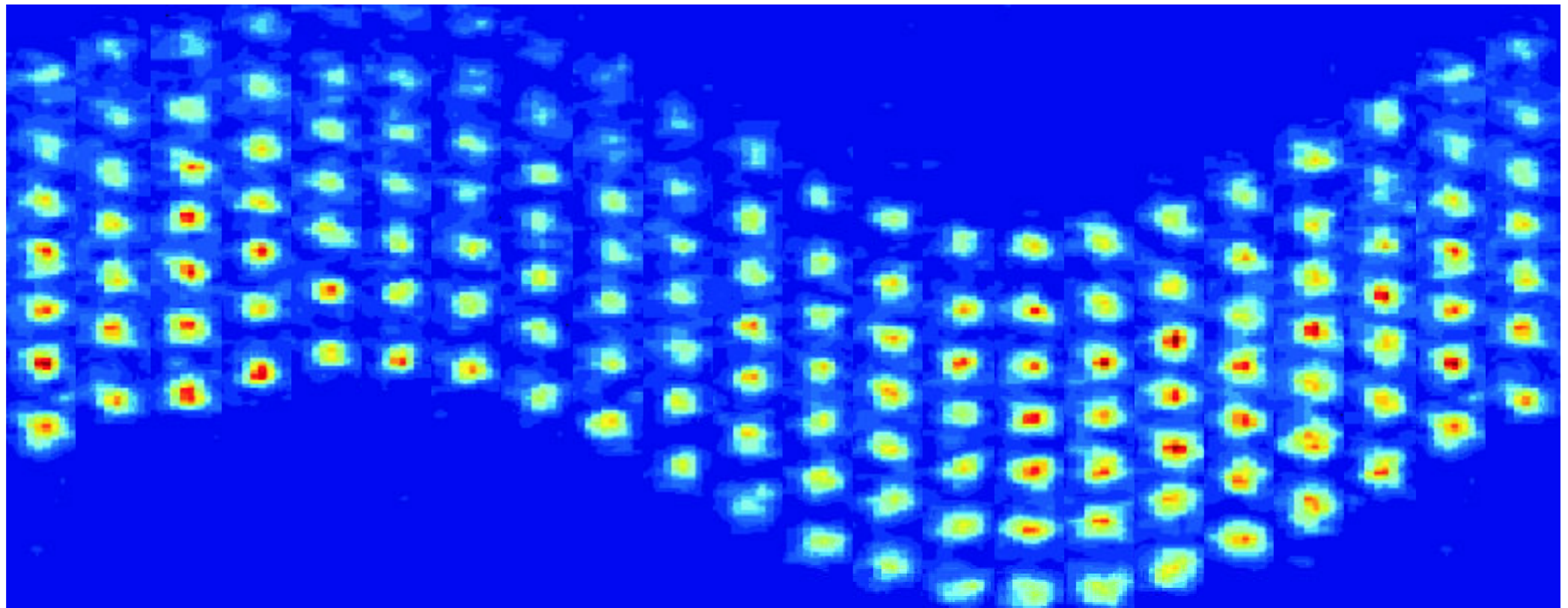


**5 ions
hot**



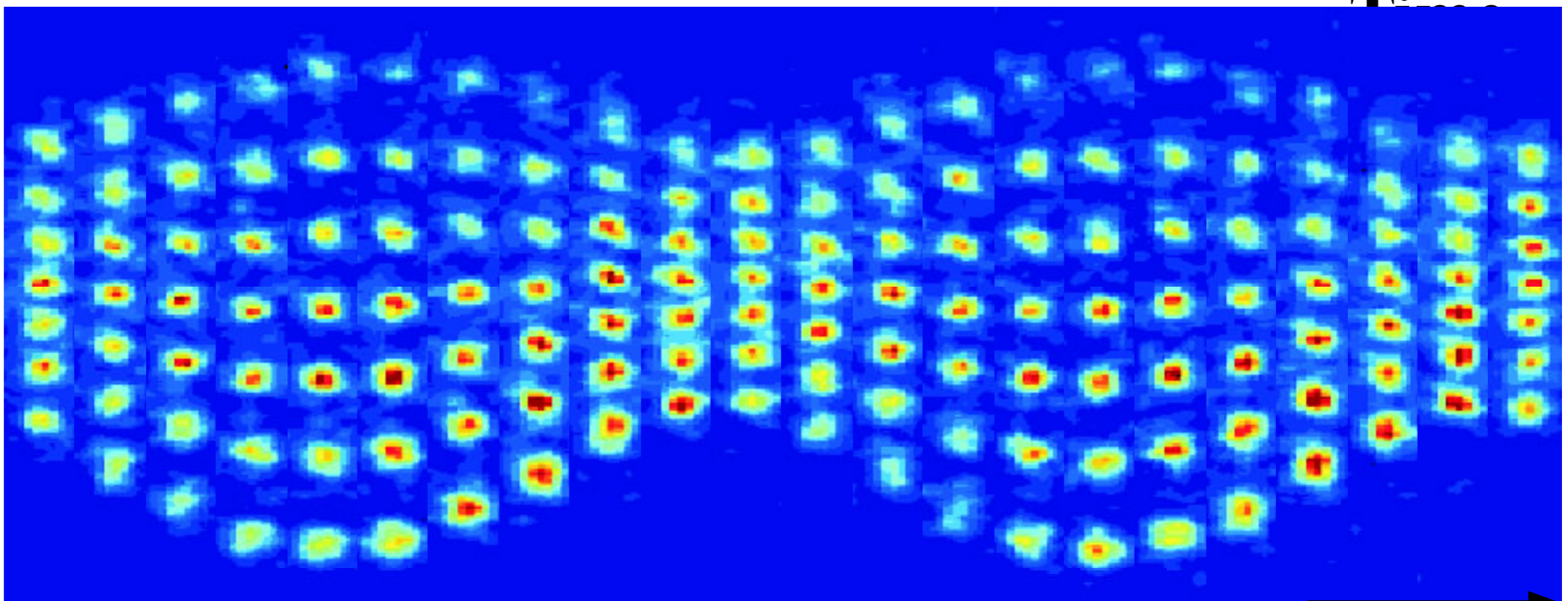
Collective Excitations

CM
106 kHz



Time →

breathing
184 kHz

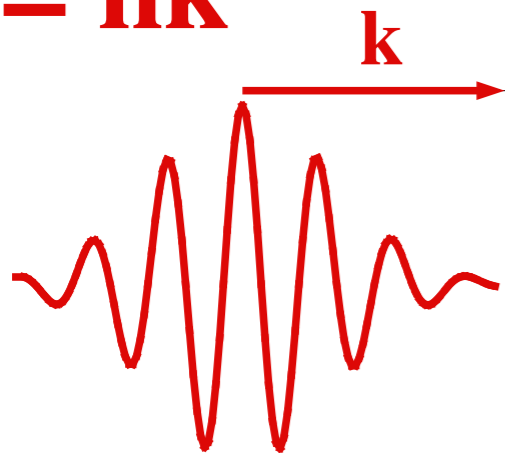


Time →

Photon Momentum

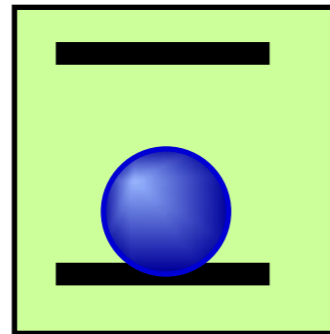
$$E = \hbar\omega$$

$$p = \hbar k$$

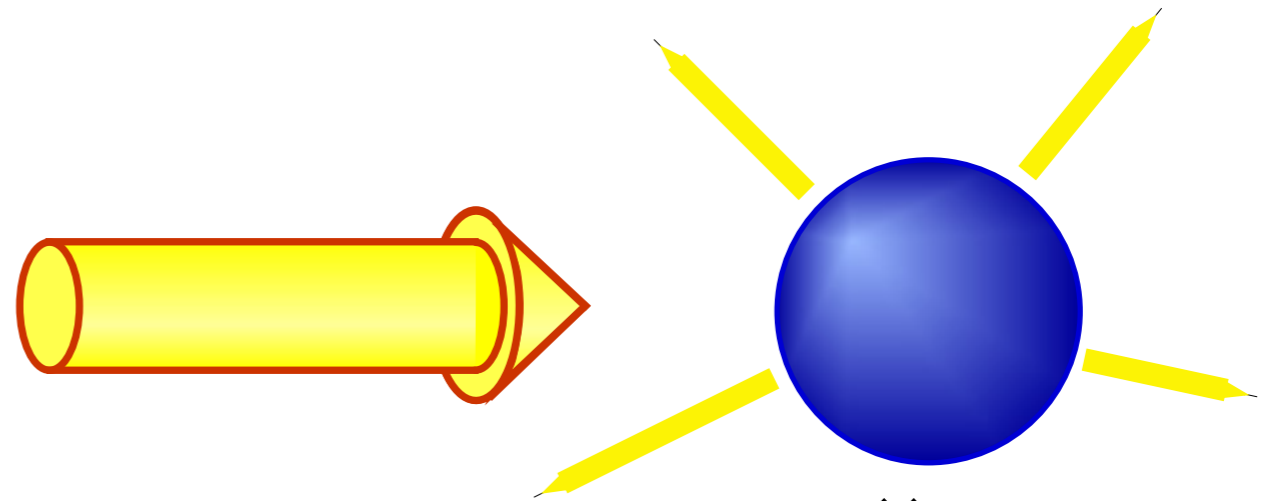


$$E = 0$$

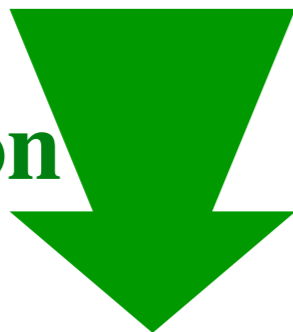
$$p = 0$$



Experimental Situation



Absorption

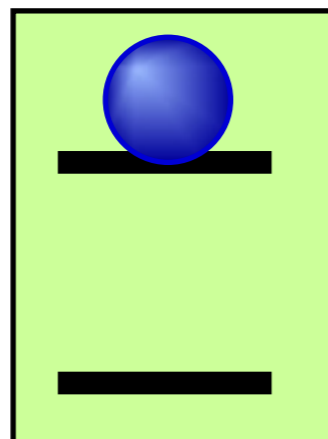


Absorption is directional } \rightarrow { Force \uparrow laserbeam
 Emission is isotropic } { average force = 0

maximum effect: $n \leq 10^8$ cycles per second

$$E = \hbar\omega$$

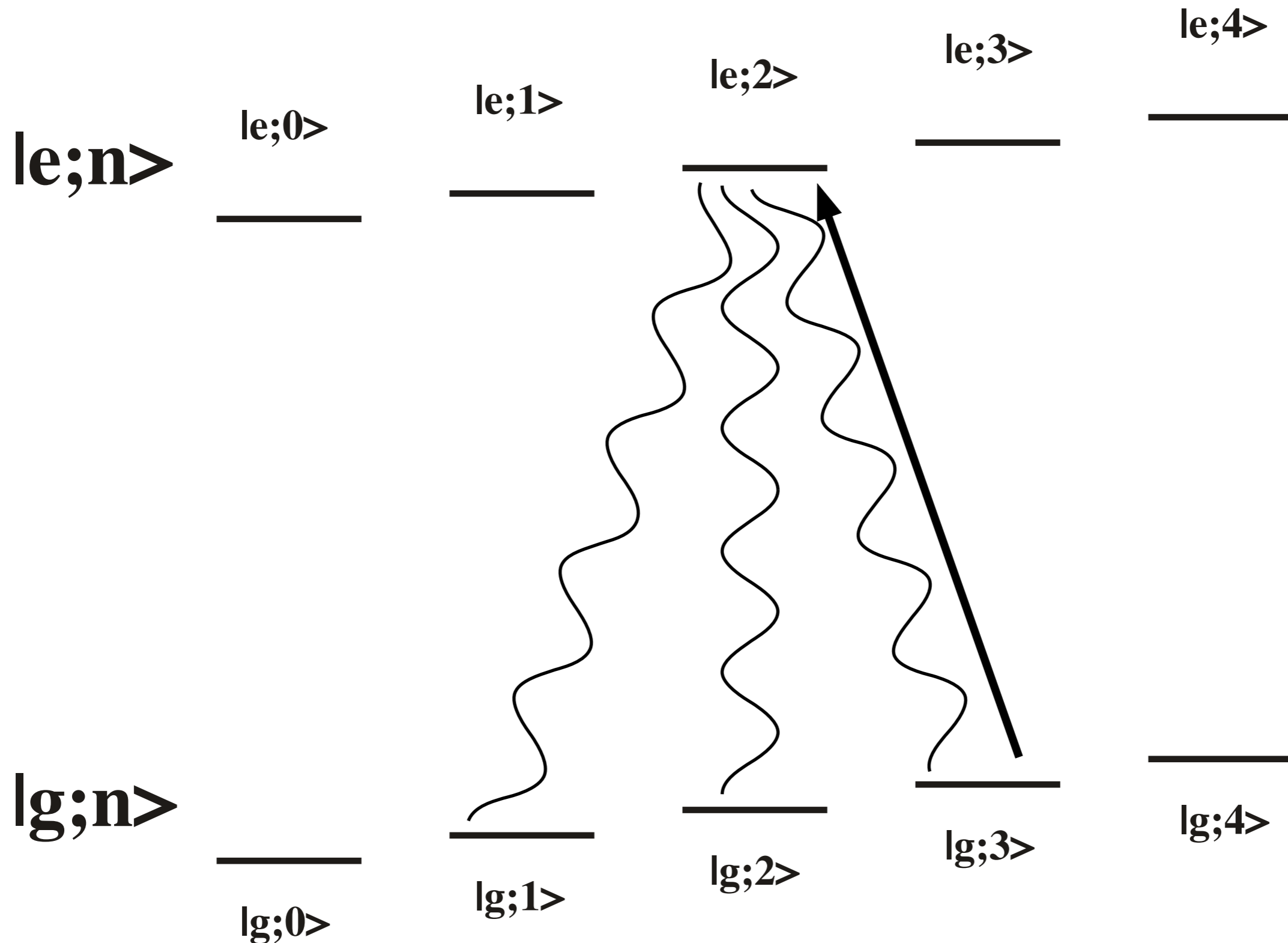
$$p = \hbar k$$



resulting acceleration =

$$\frac{n \hbar k}{\text{sec } M_{\text{atom}}} = 1.7 \cdot 10^6 \frac{\text{m}}{\text{sec}^2}$$

Sideband Cooling



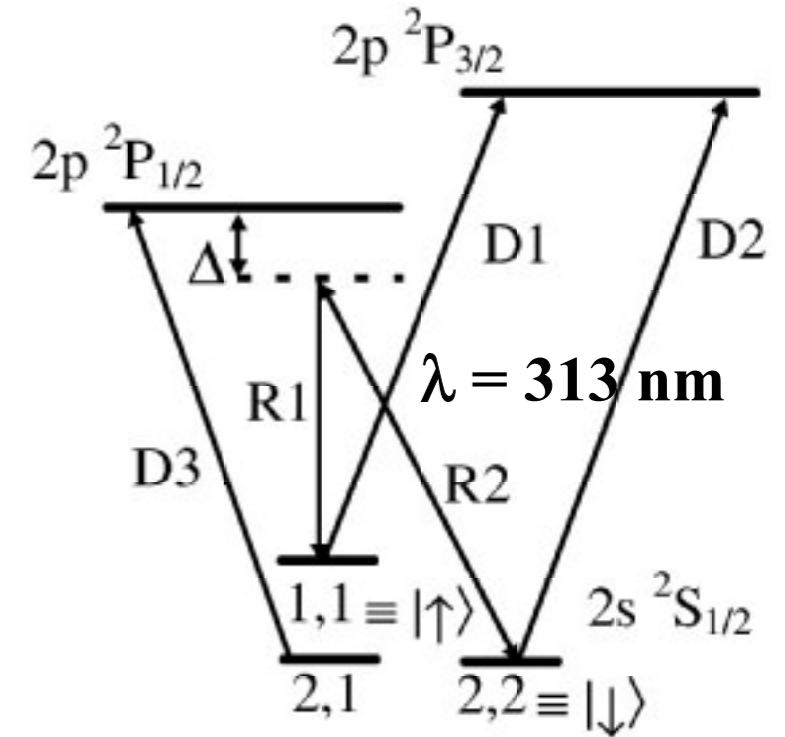
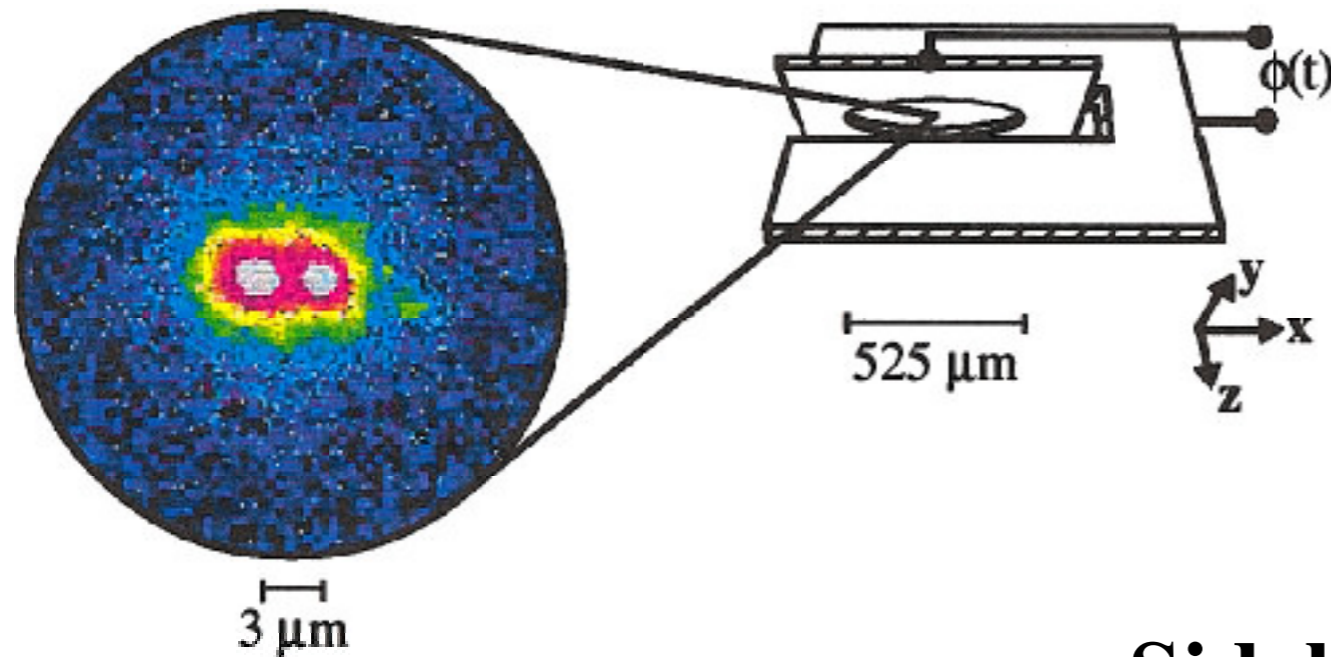
Use Raman pulses to eliminate Doppler broadening

Sideband Cooling

${}^9\text{Be}^+$

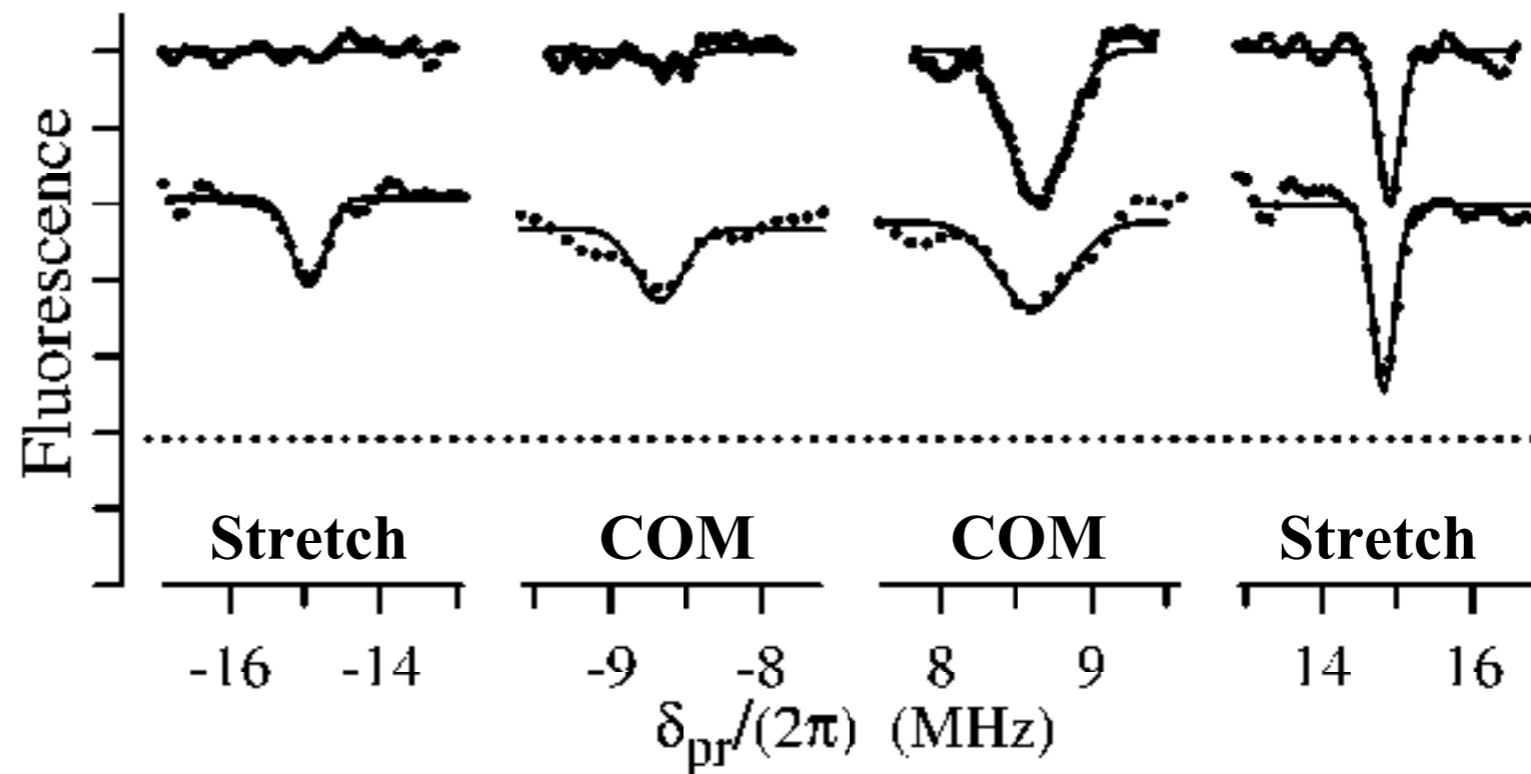
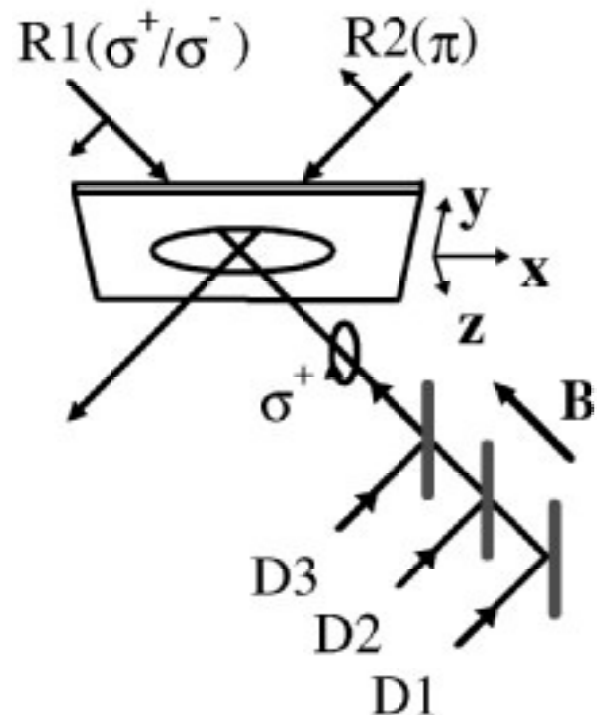
Microtrap : $(\omega_x, \omega_y, \omega_z) = (8.6, 17.6, 9.3)$ MHz

Transitions:



Sidebands:

Cooling:

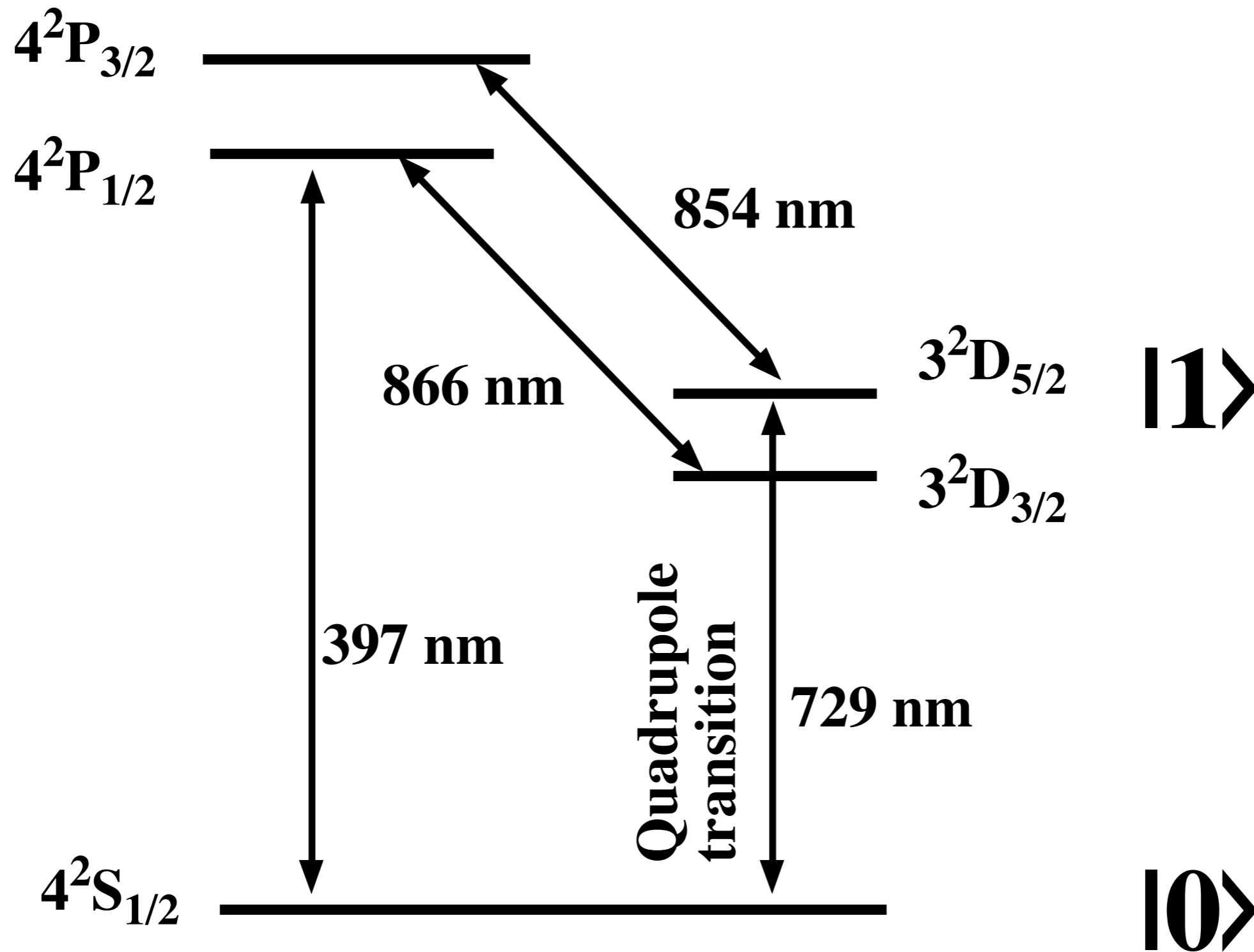


Sideband cooling

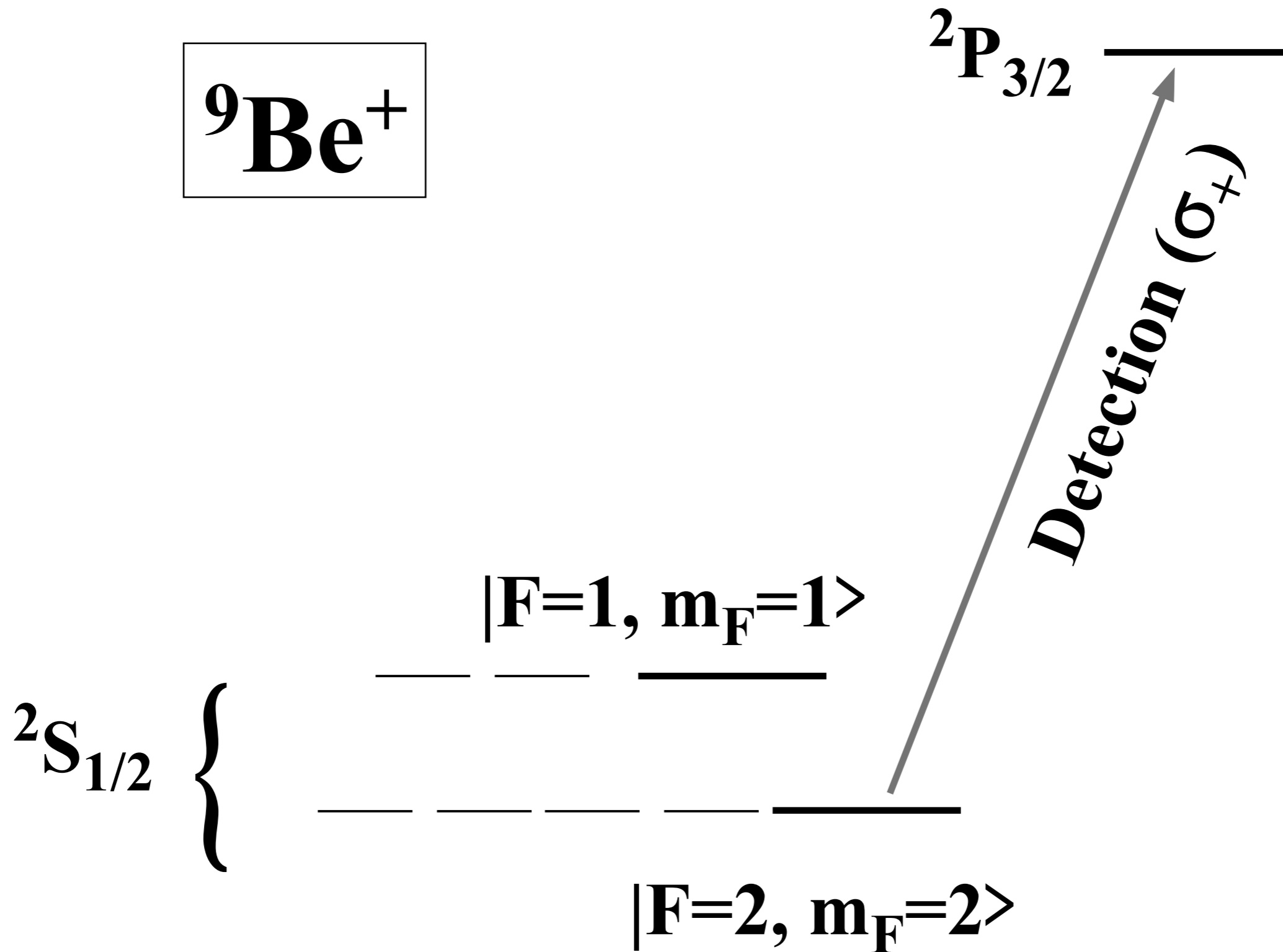
Doppler cooling

King et al., PRL 81, 1525 (1998).

Ca⁺ Qubit



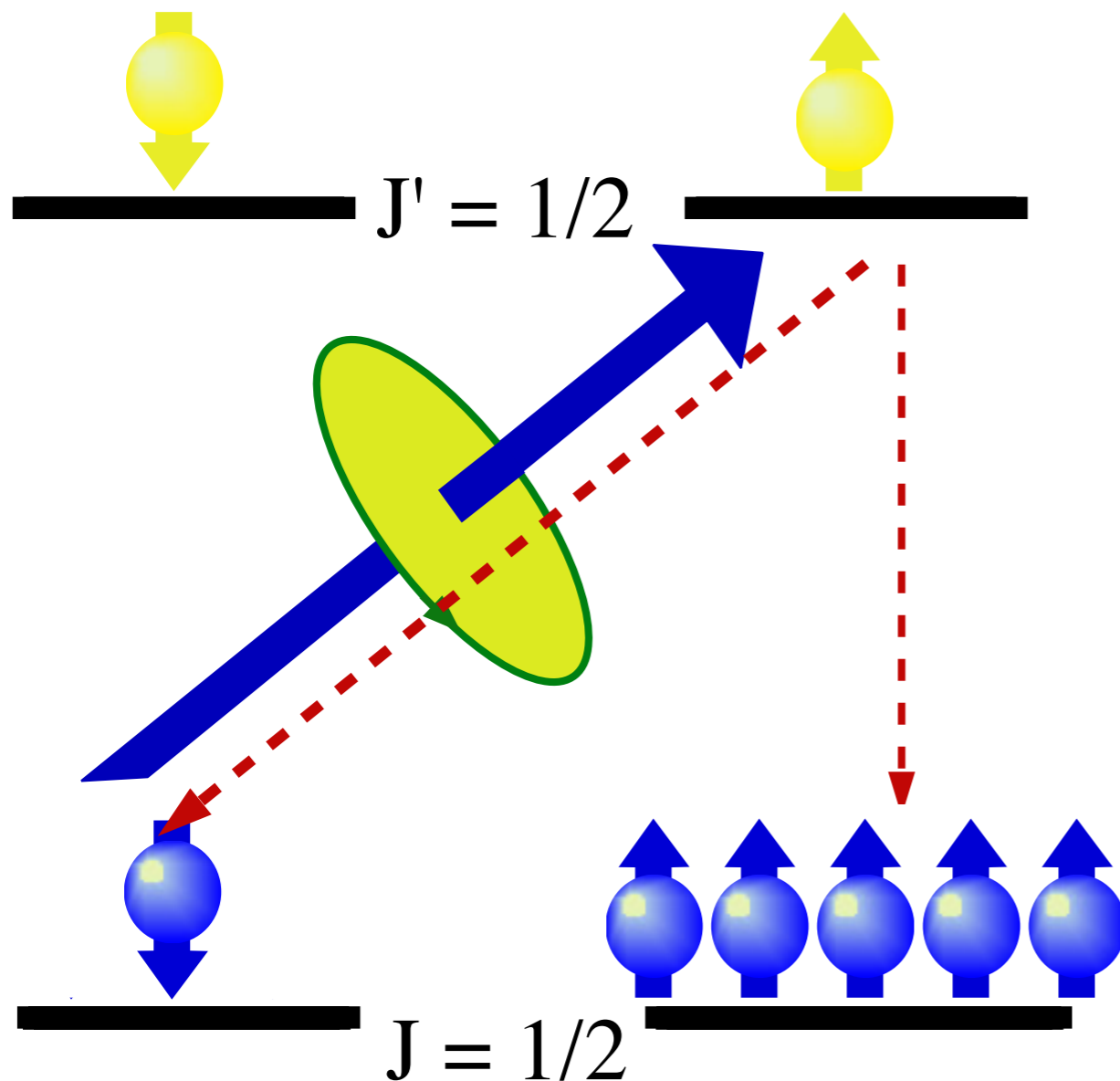
Be⁺ Qubit



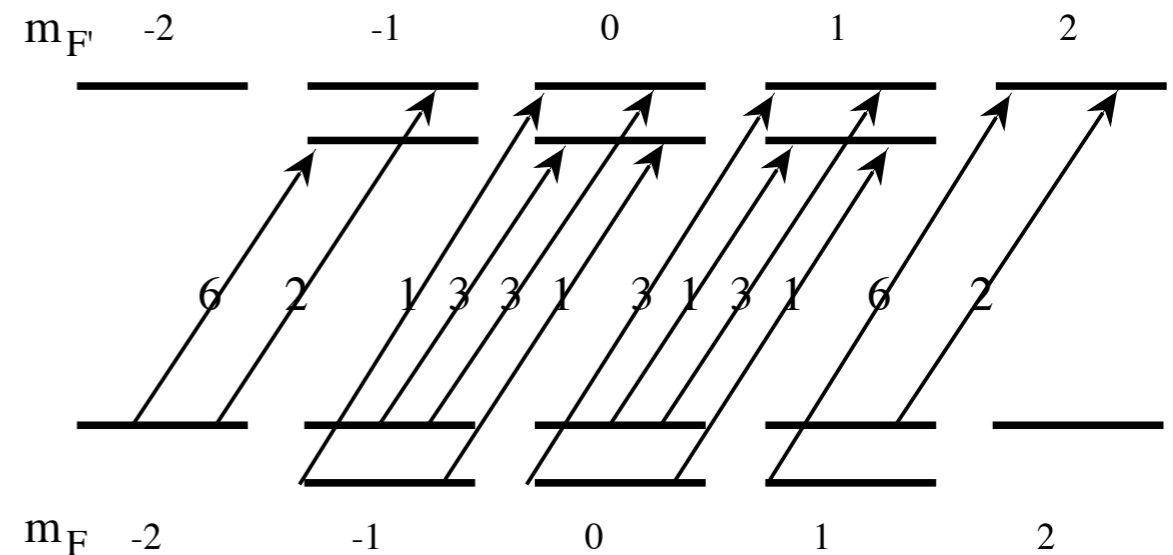
Optical Pumping

Principle:

A. Kastler, J. Phys. 11, 255 (1950)

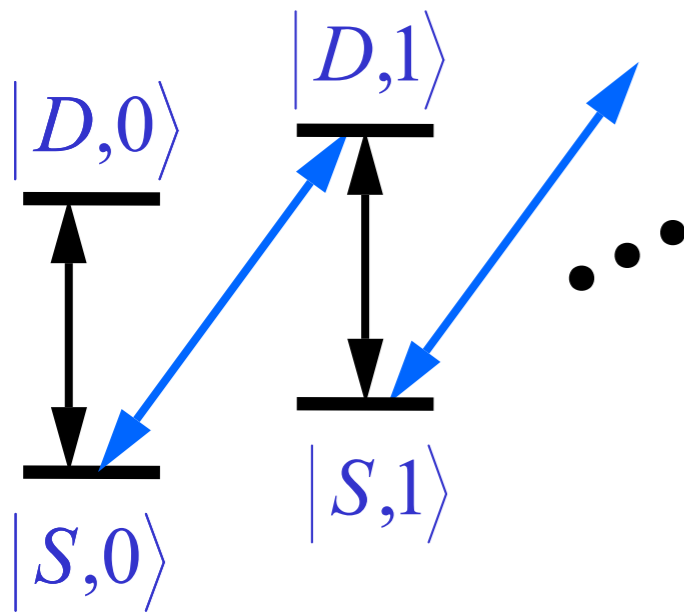


Multilevel system:



Two Qubit Gate

$^{40}\text{Ca}^+$

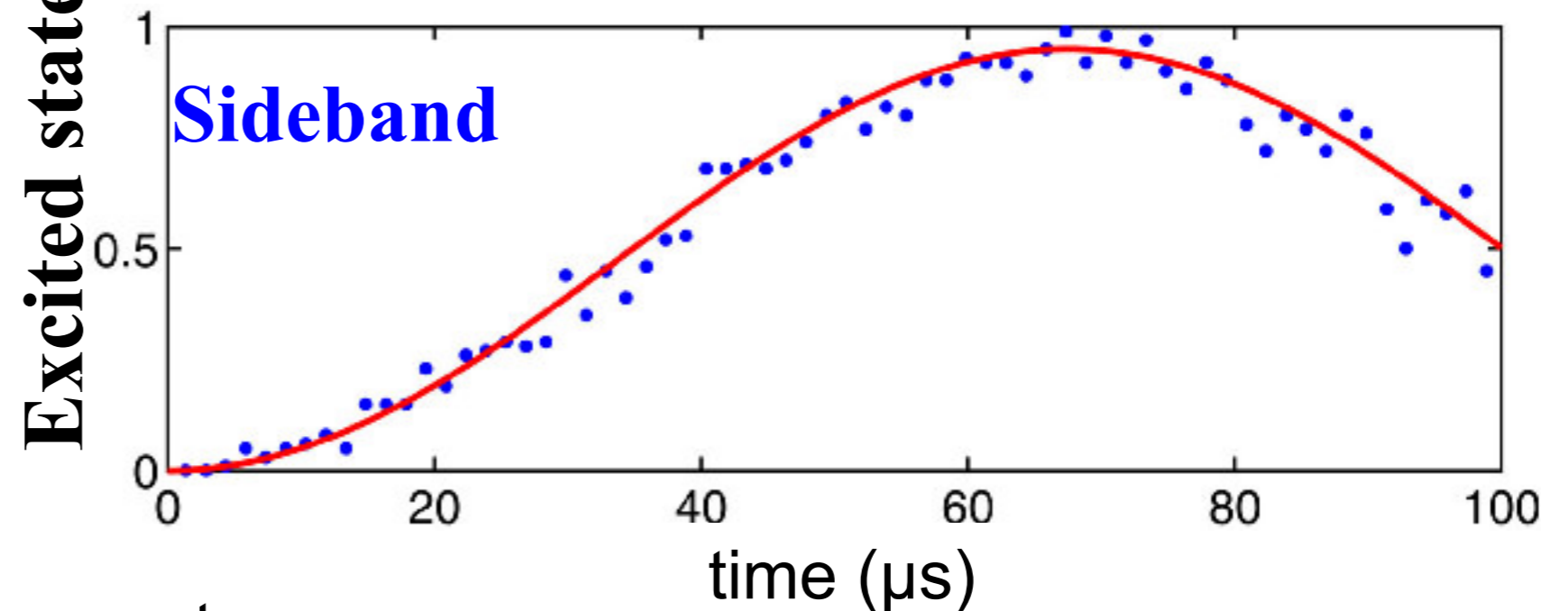
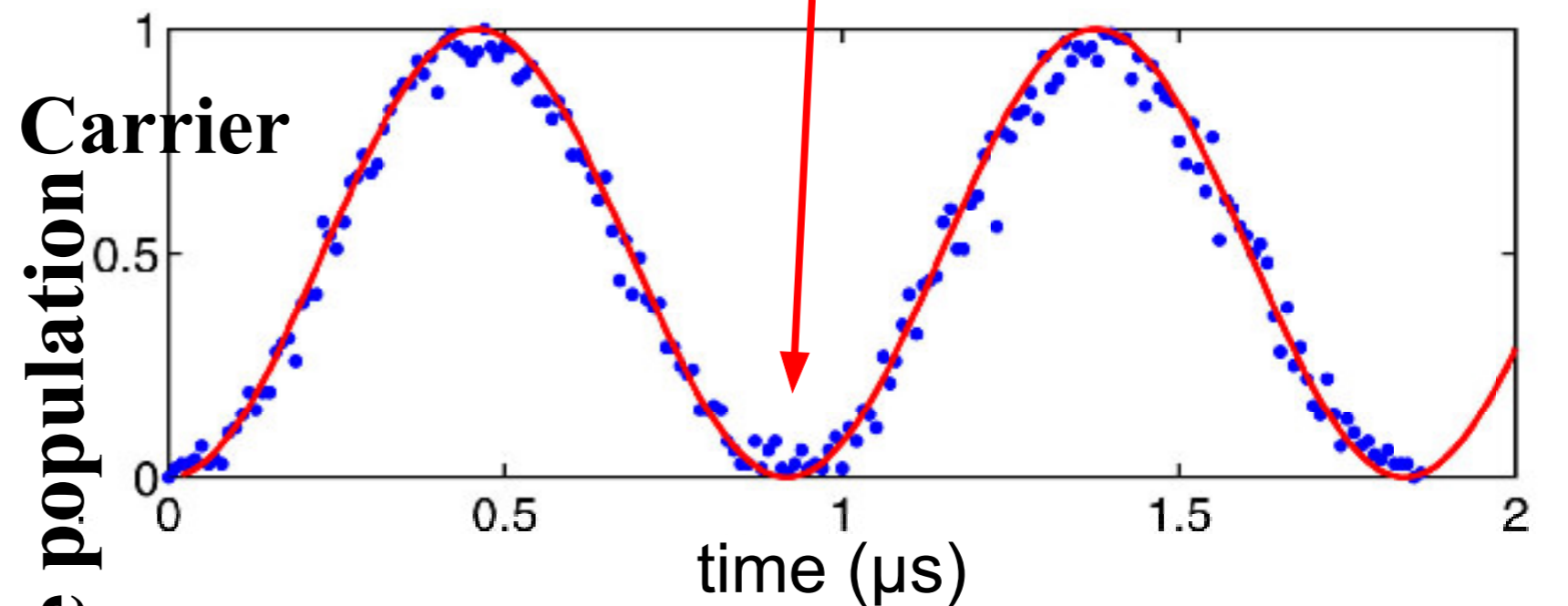


carrier and **sideband**
Rabi oscillations
with Rabi frequencies

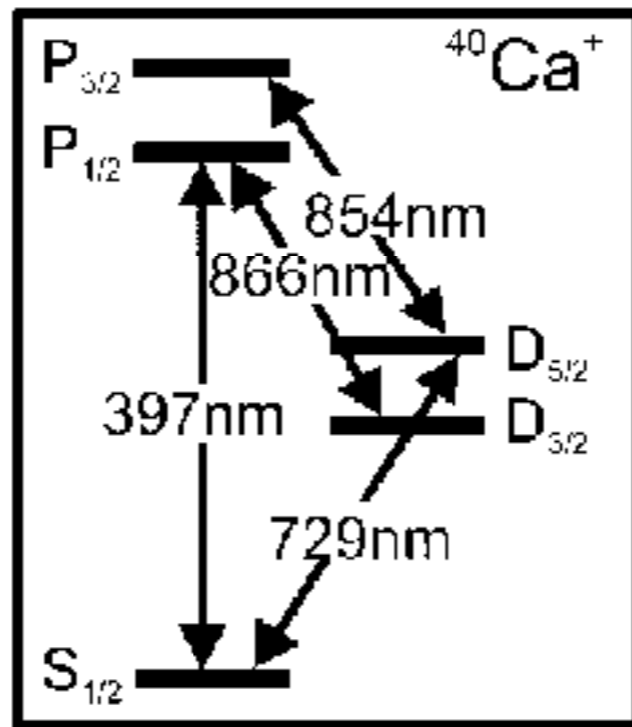
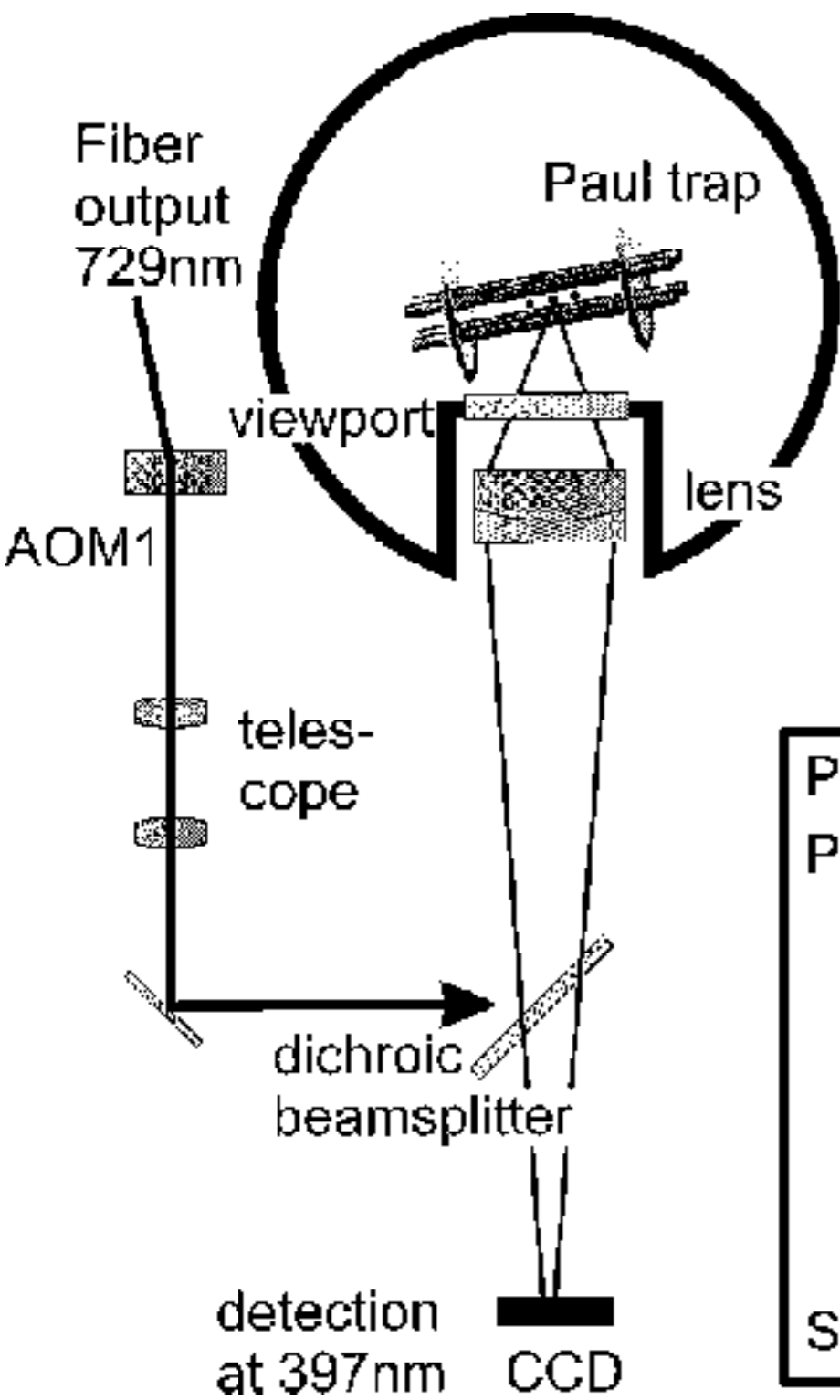
$$\Omega, \quad \eta\Omega\sqrt{n+1}$$

$\eta = kx_0$ Lamb-Dicke parameter

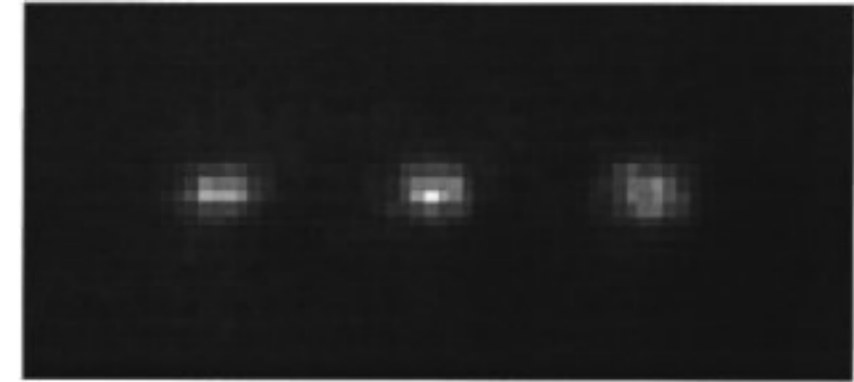
$2 = 1$



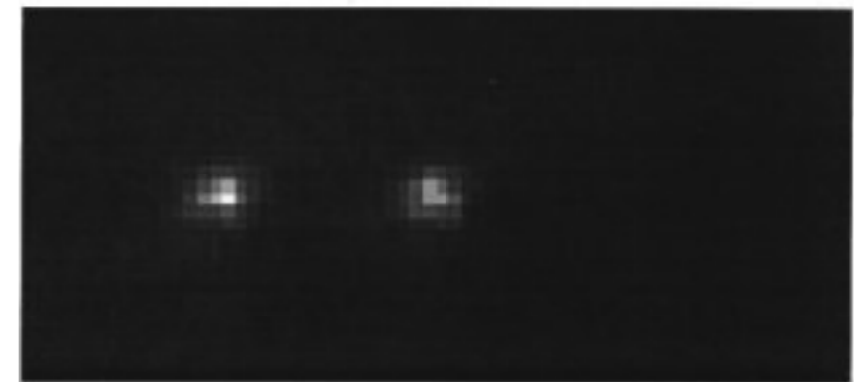
Addressing



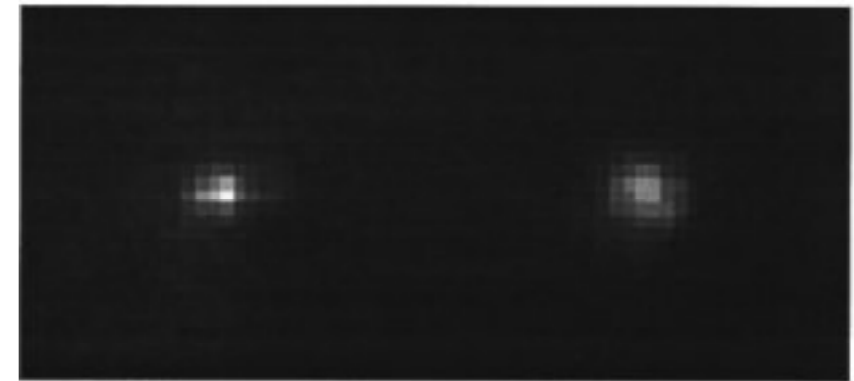
$|111\rangle$



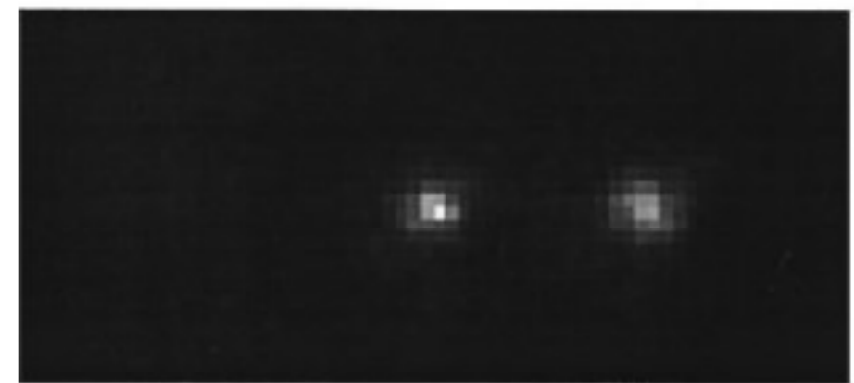
$|110\rangle$



$|101\rangle$

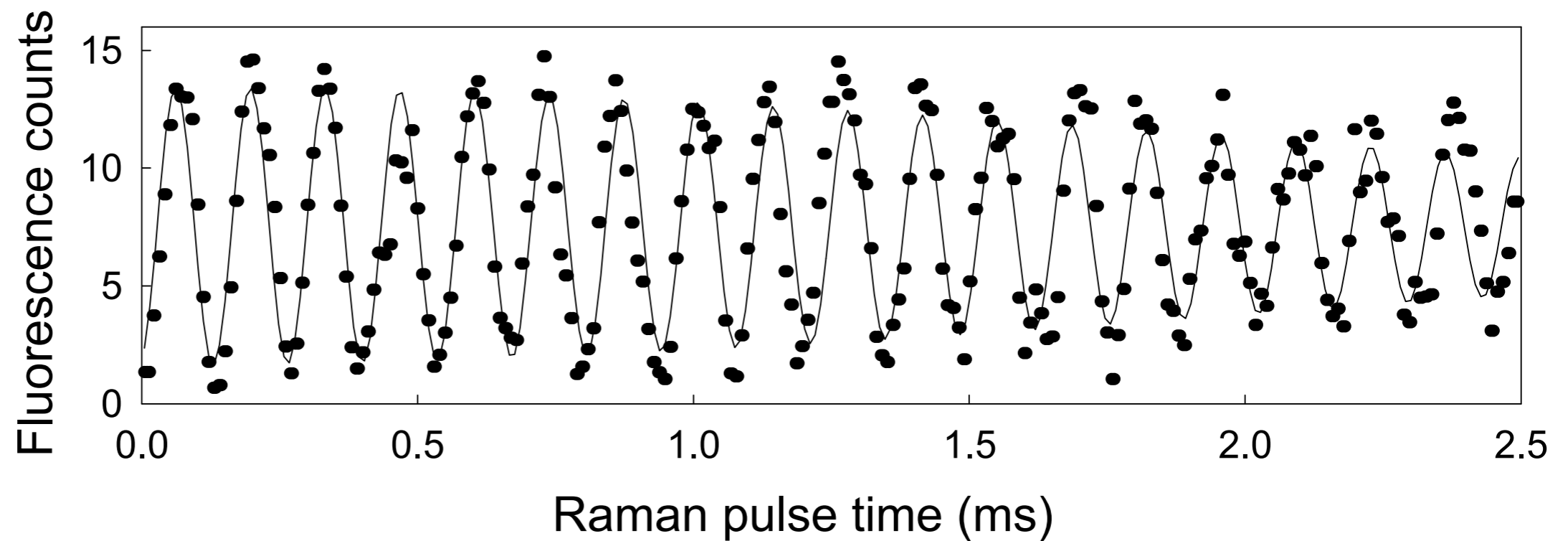
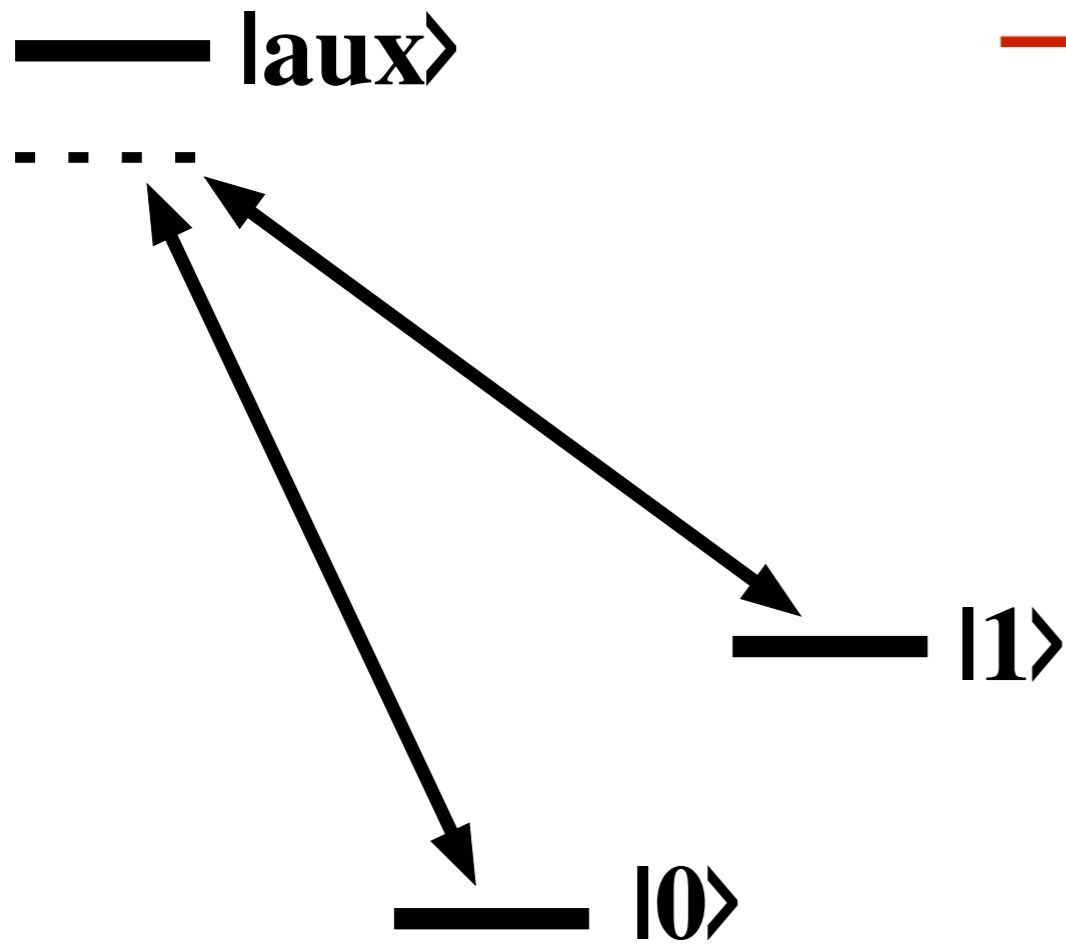


$|011\rangle$

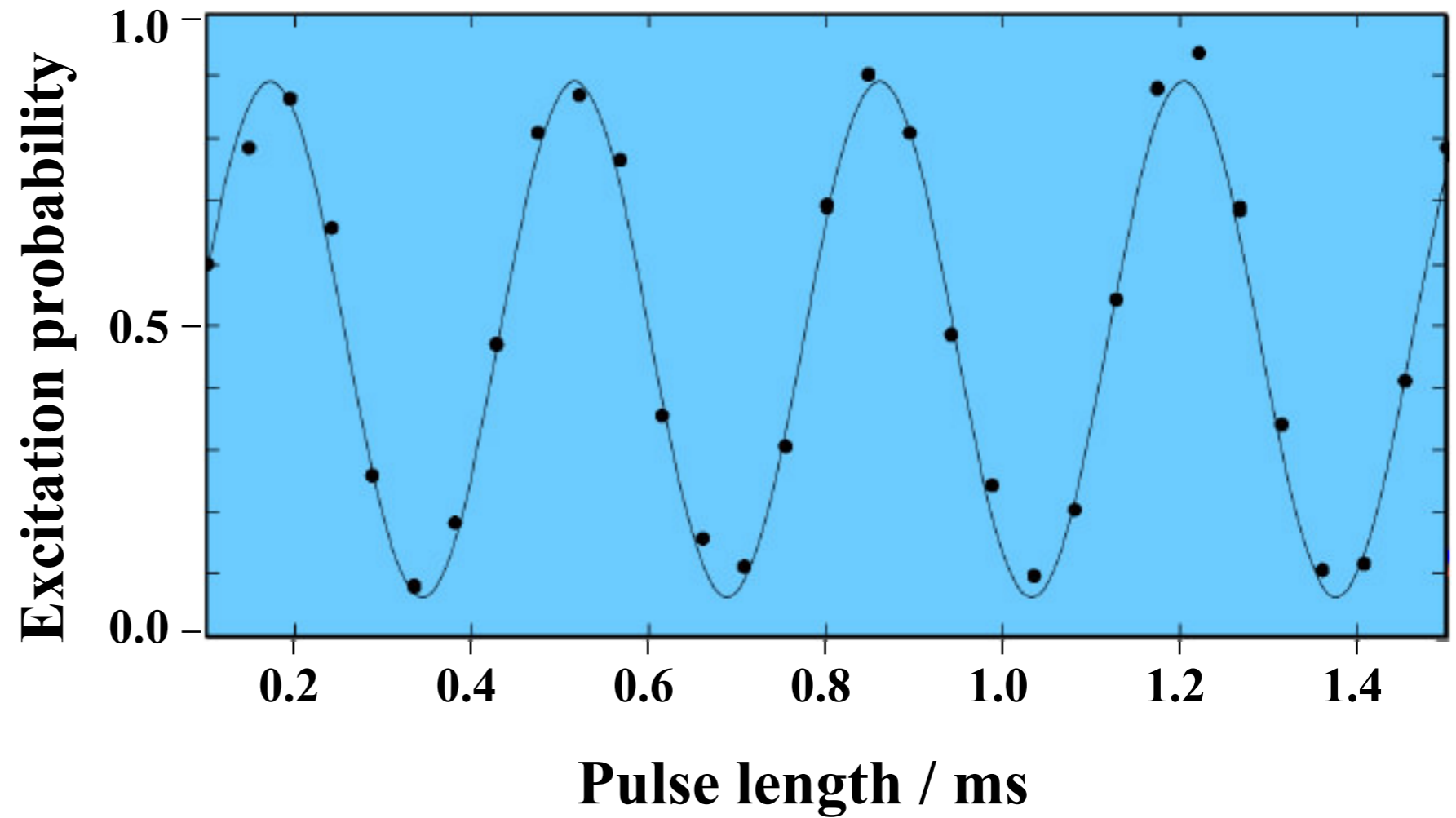
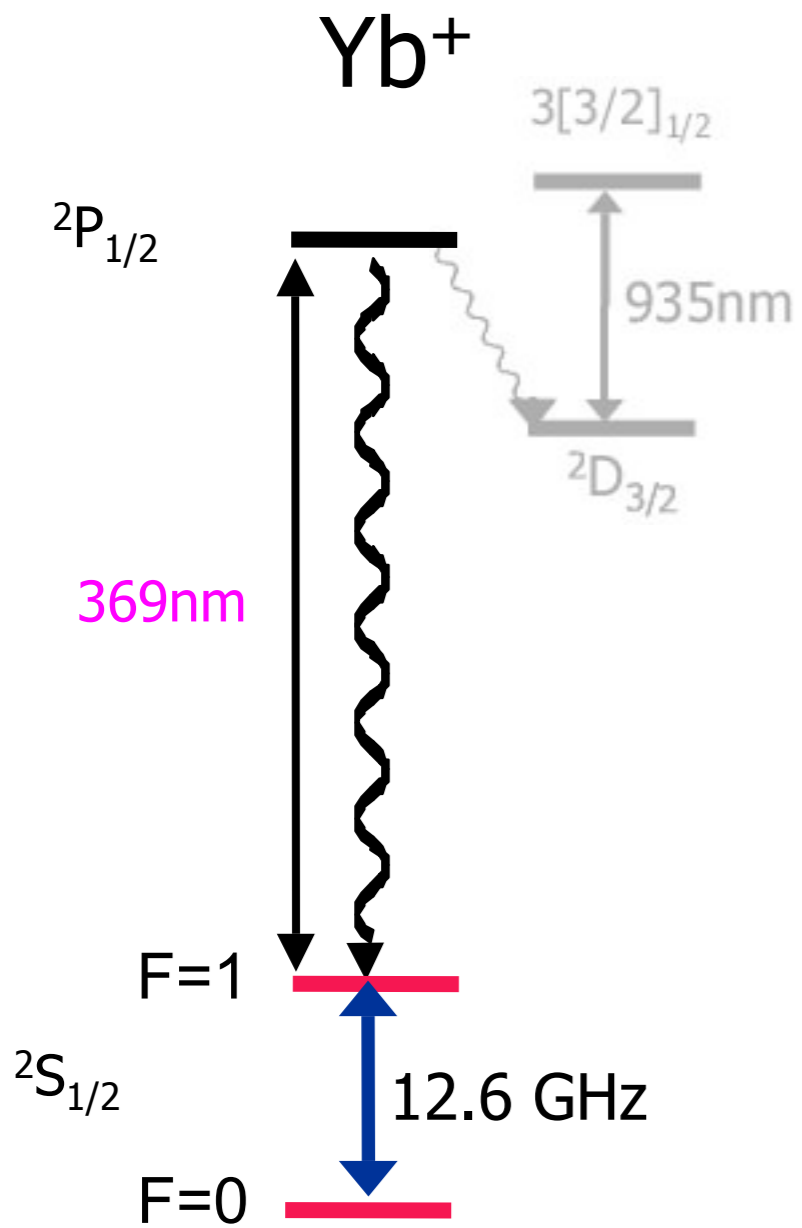


20 μm

Raman Laser Pulse

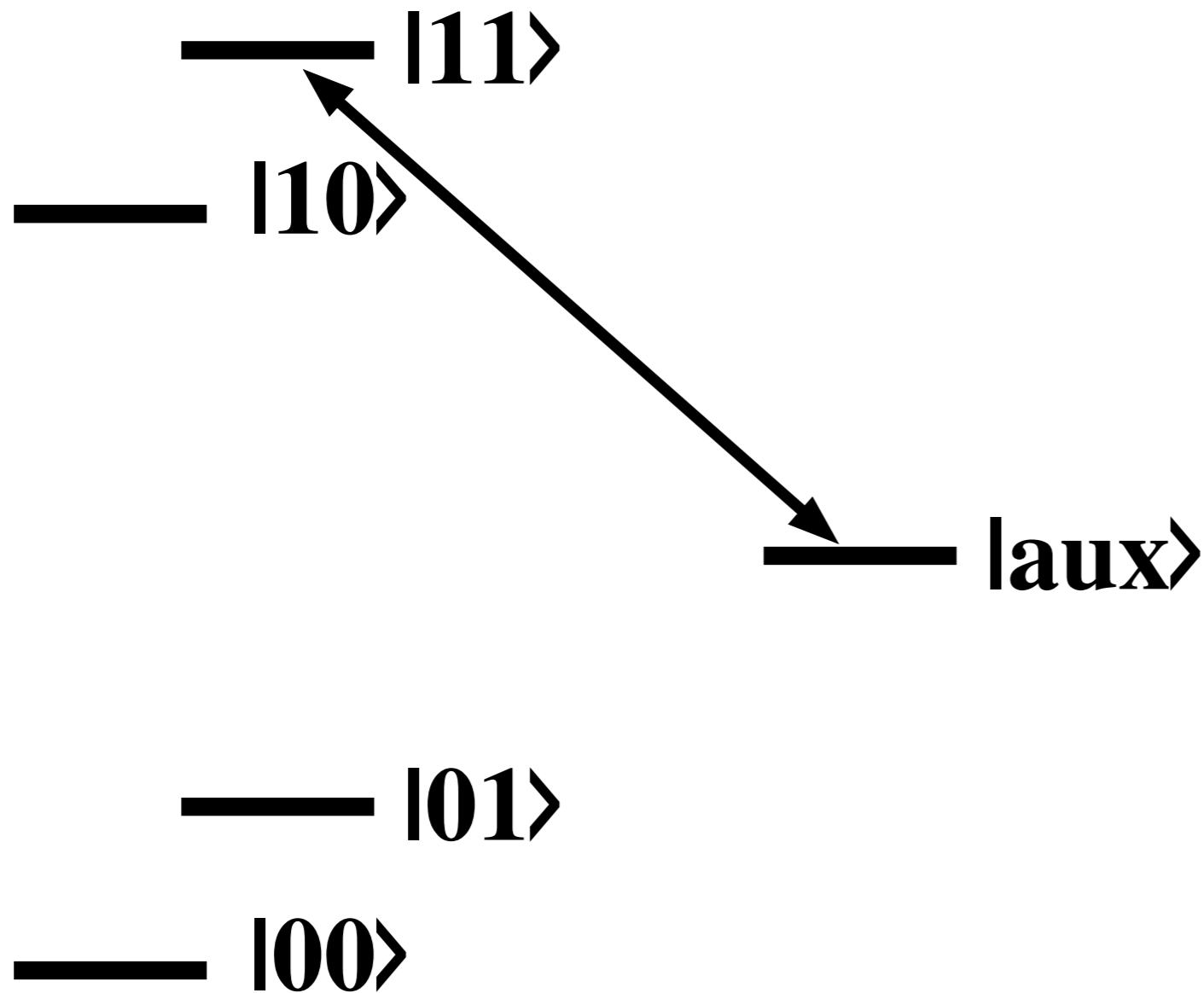


Microwave Pulse

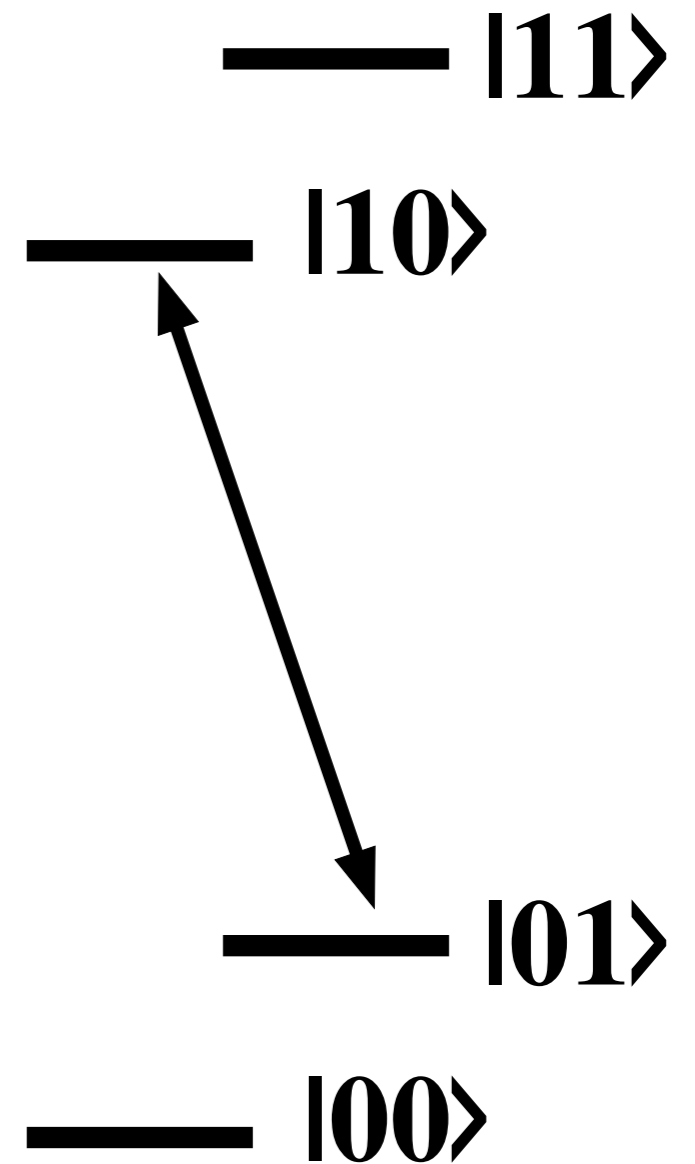


Two Qubit Gates

Phase gate

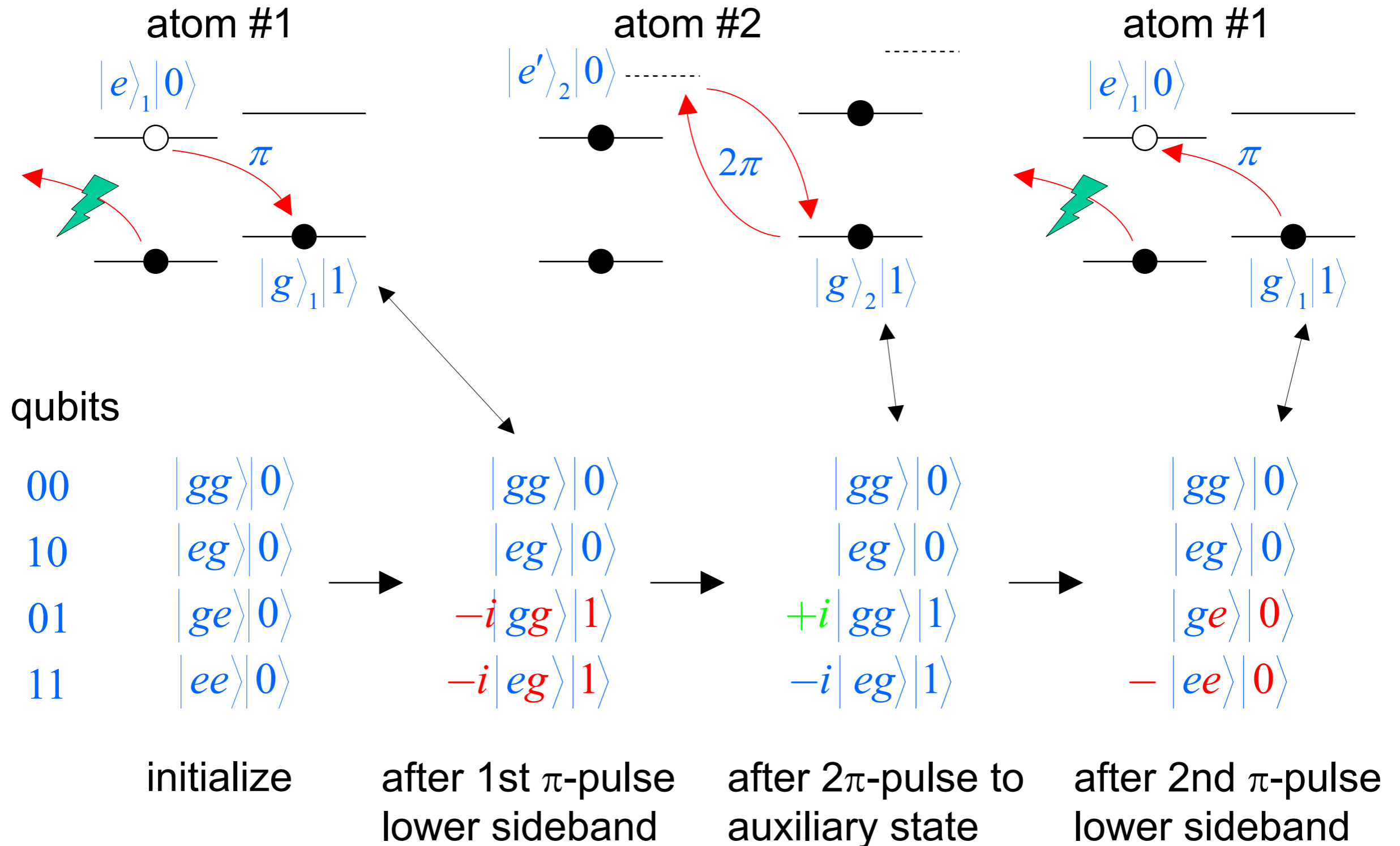
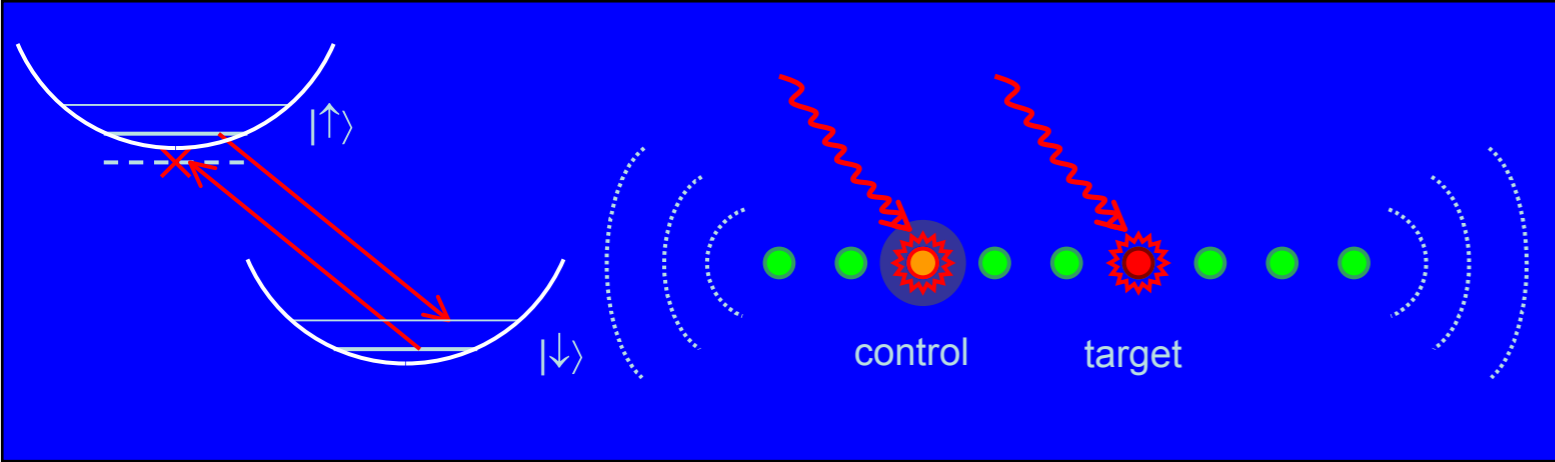


SWAP

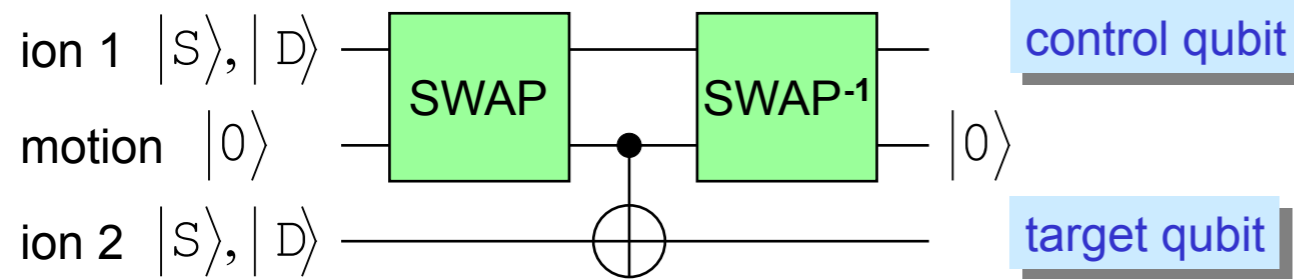
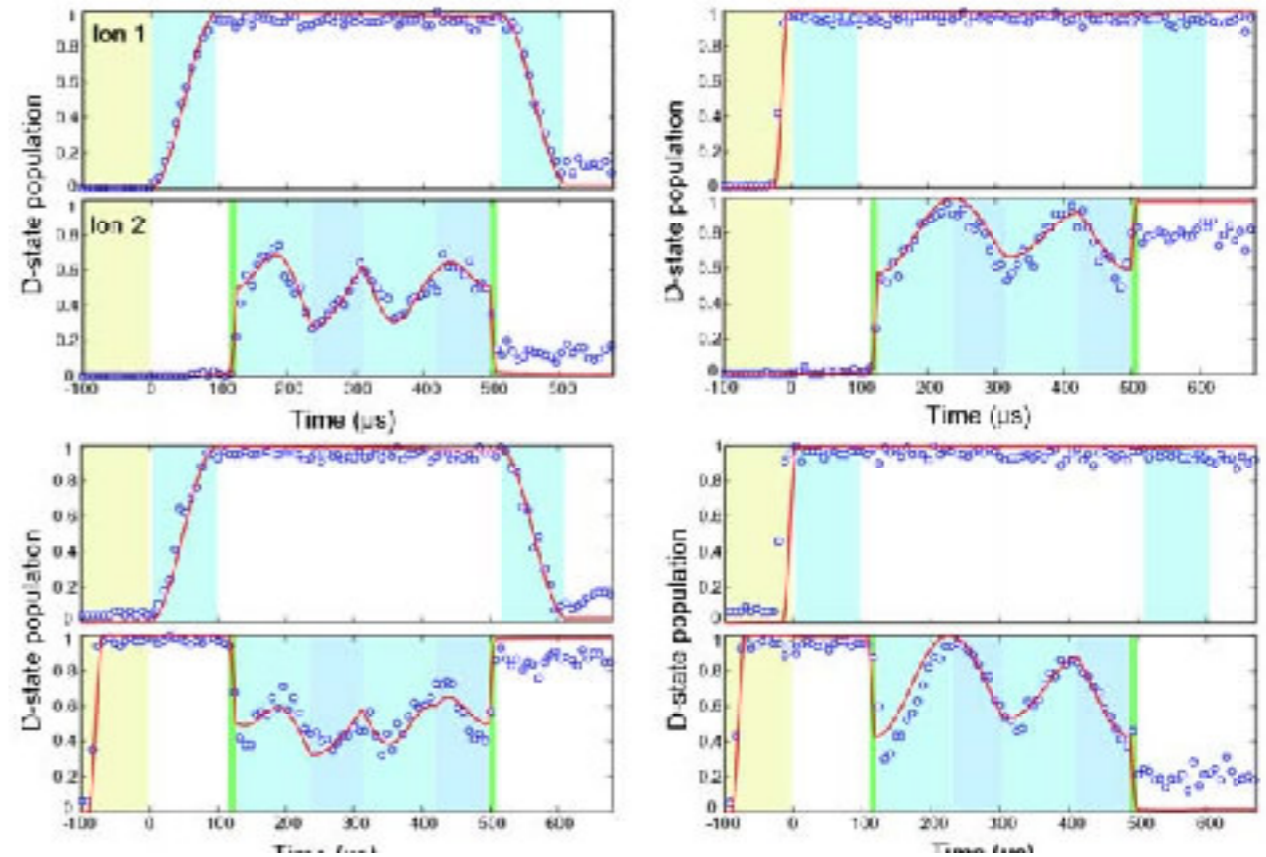
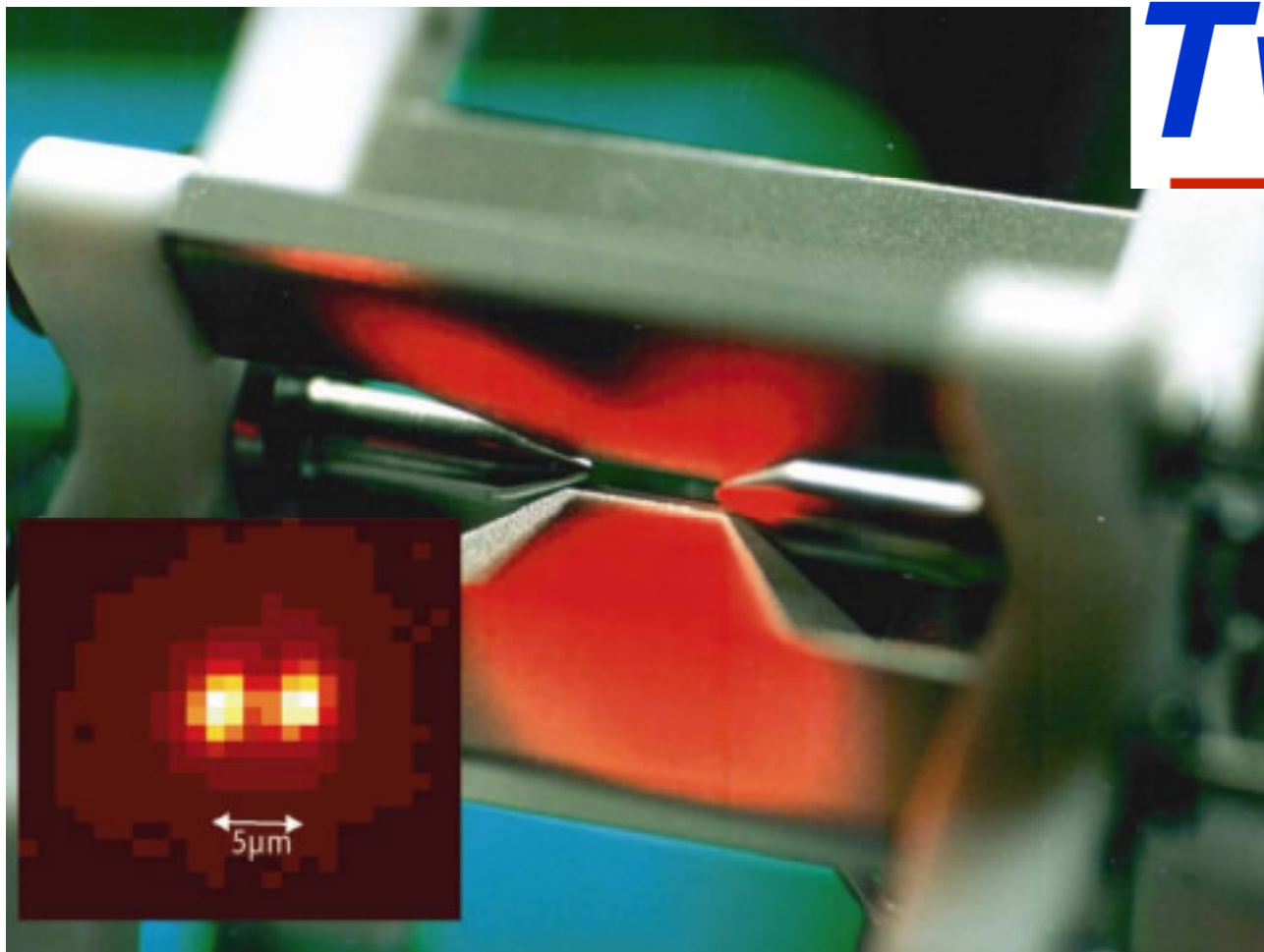


C Phase

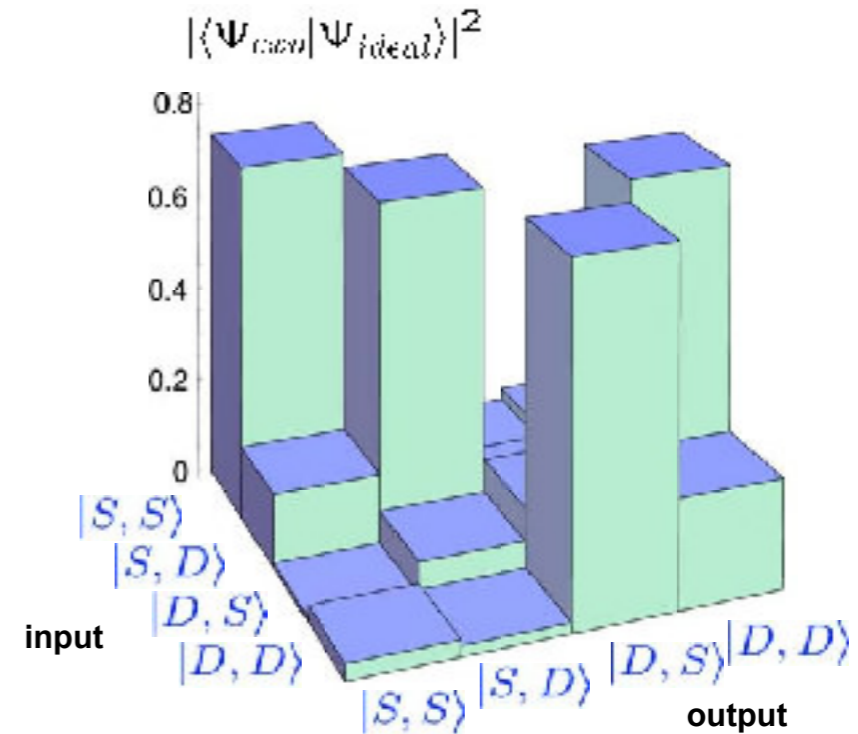
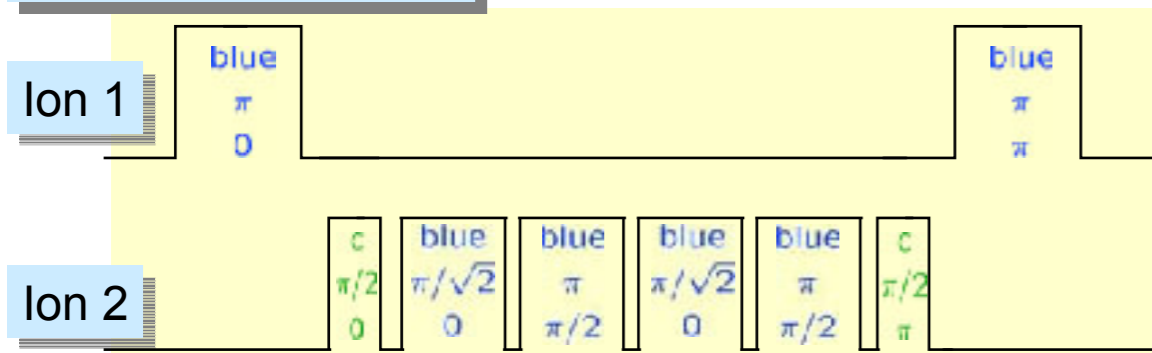
Cirac & Zoller, PRL 74, 4091 (1995)



Two Qubit Gates

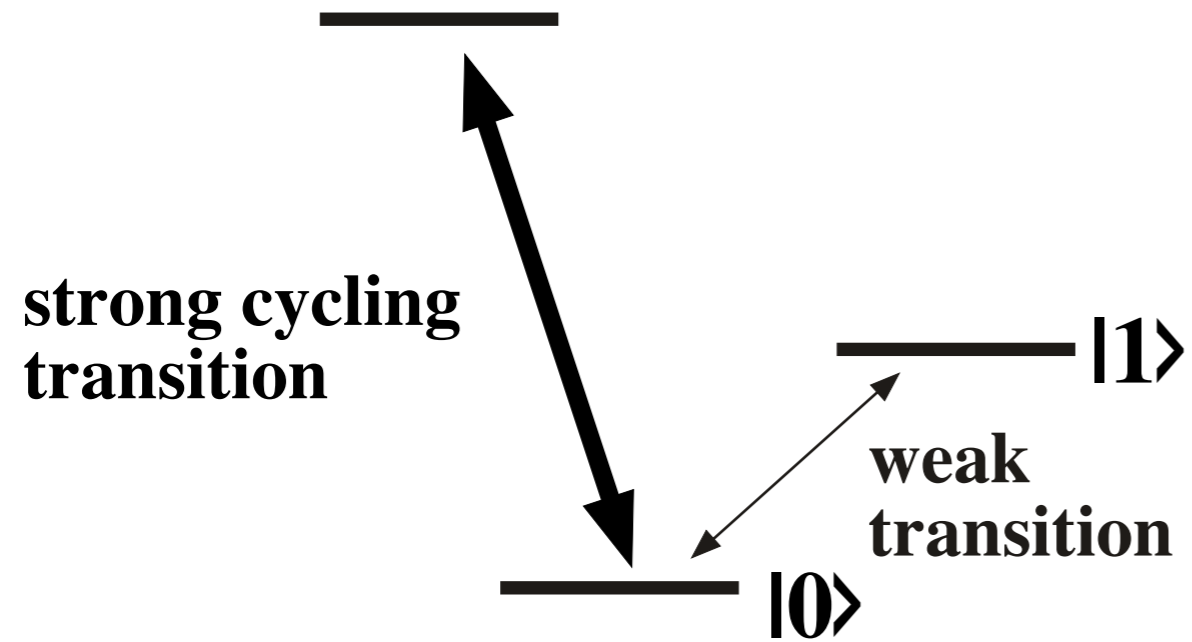


pulse sequence:

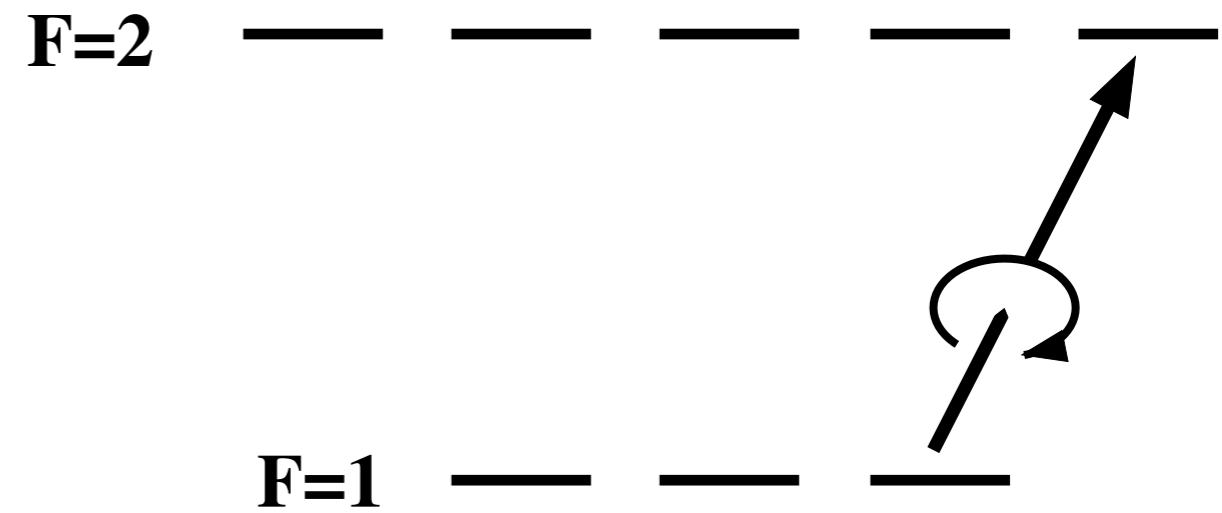


Schmidt-Kaler et al., *Nature* **422**, 408 (2003)

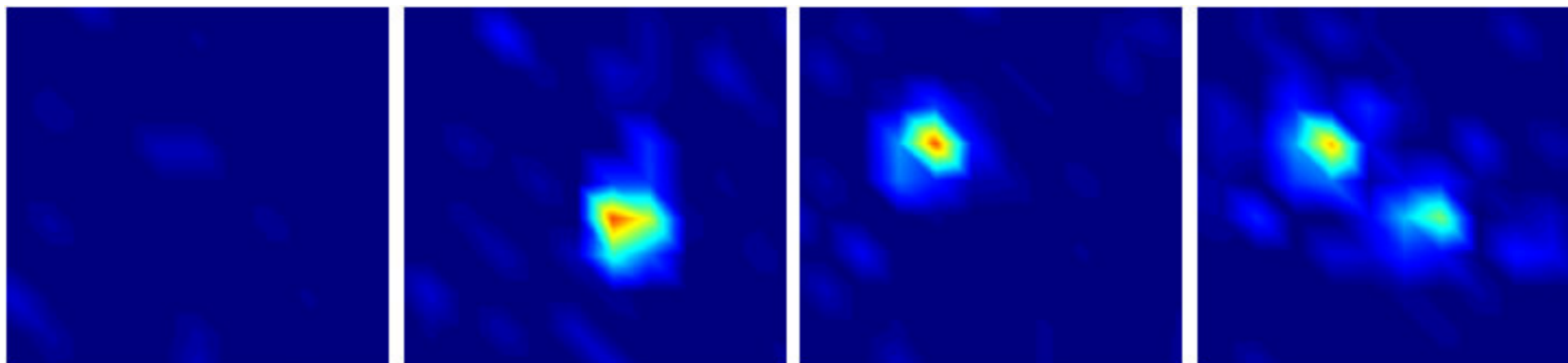
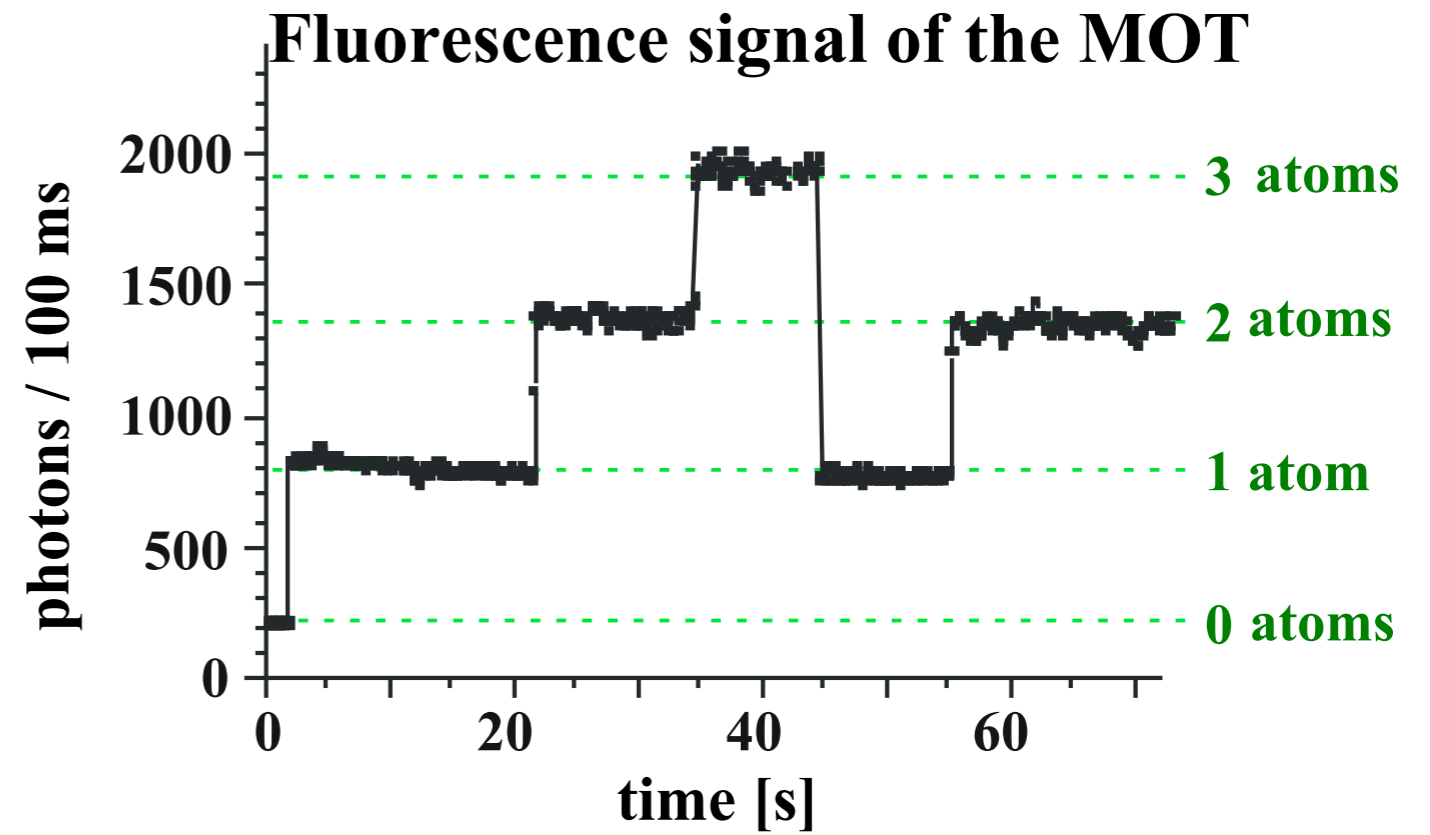
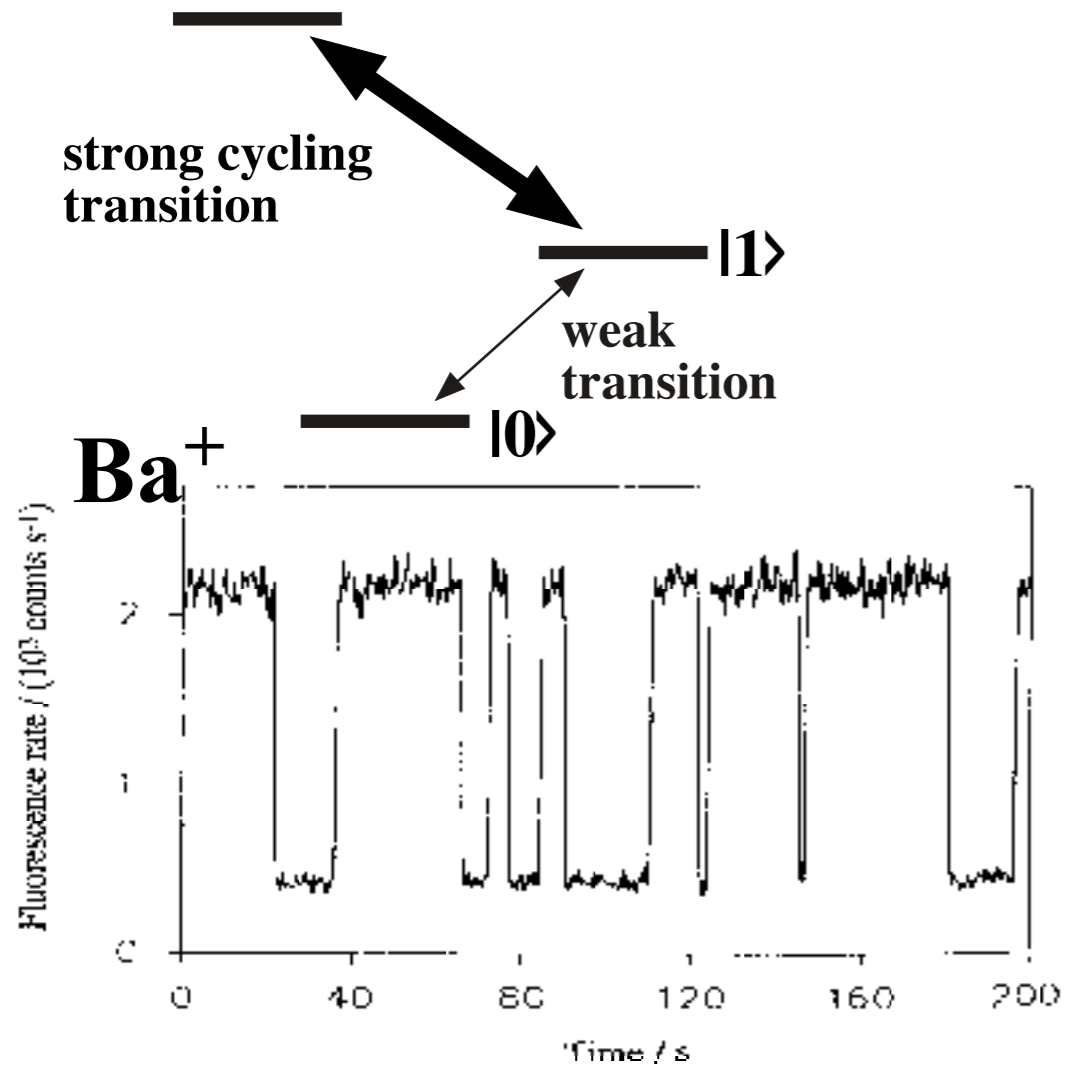
Readout



Cycling transition



Fluorescence of Single Ion



$|00\rangle$

$|01\rangle$

$|10\rangle$

$|11\rangle$

5 Qubit Quantum Register

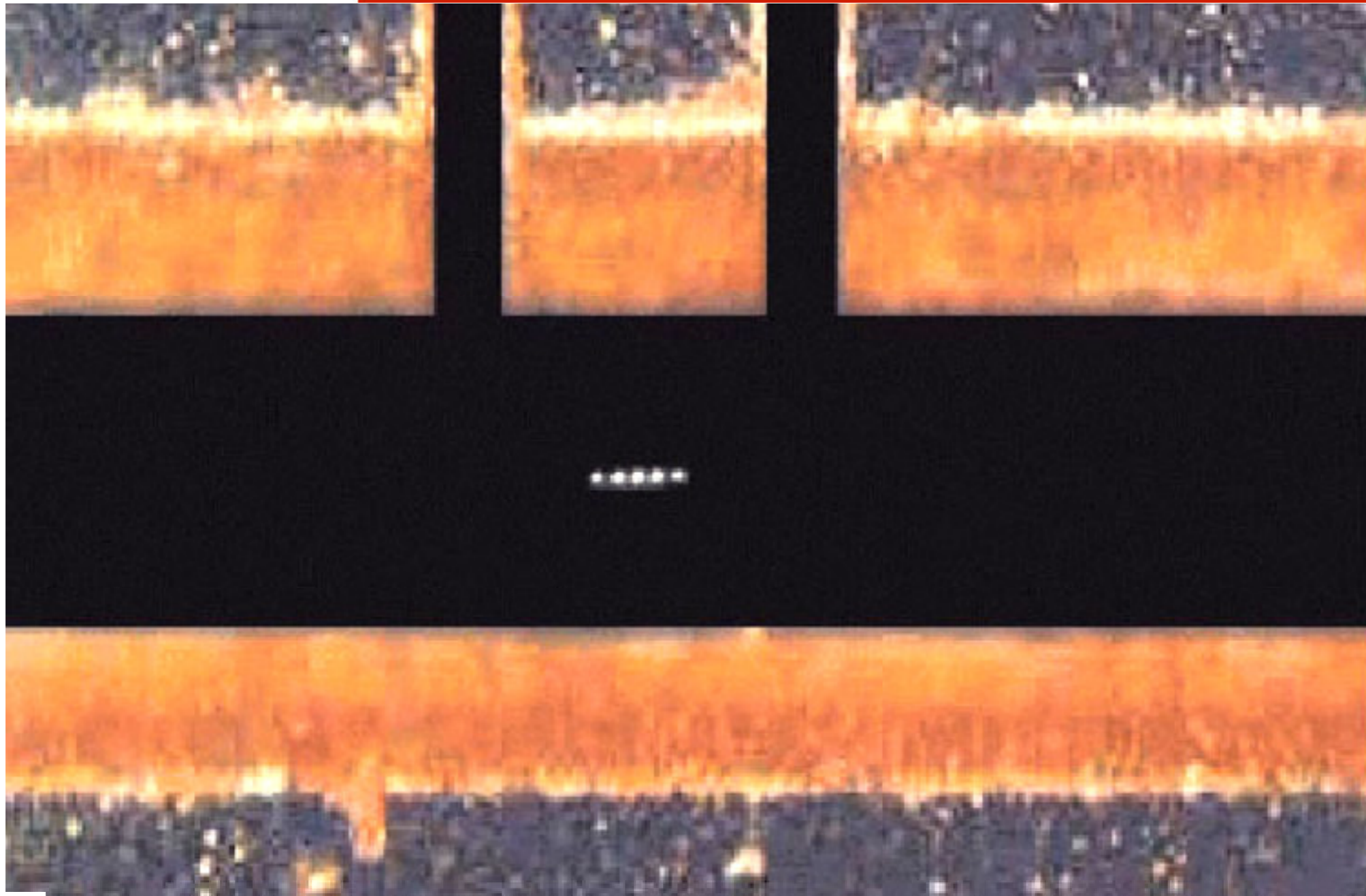
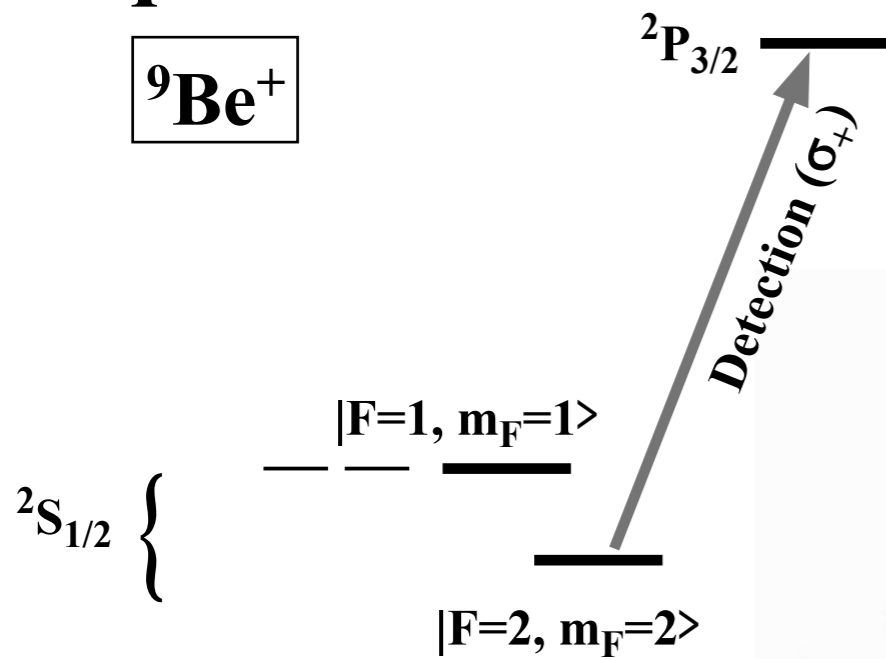


Figure 2 A crystal of five atomic beryllium ions (small white dots at centre) confined in a radio-frequency ion trap. The ions balance their mutual Coulomb repulsion with the confining force of electric fields generated from the surrounding electrodes (brown). The ions strongly fluoresce under the application of appropriate laser radiation near 313 nm. The horizontal electrode gap is about 0.2 mm and the ion–ion spacing is $\sim 5 \mu\text{m}$. (Image courtesy of NIST, Boulder.)

Exp. CNOT Gate on ${}^9\text{Be}^+$

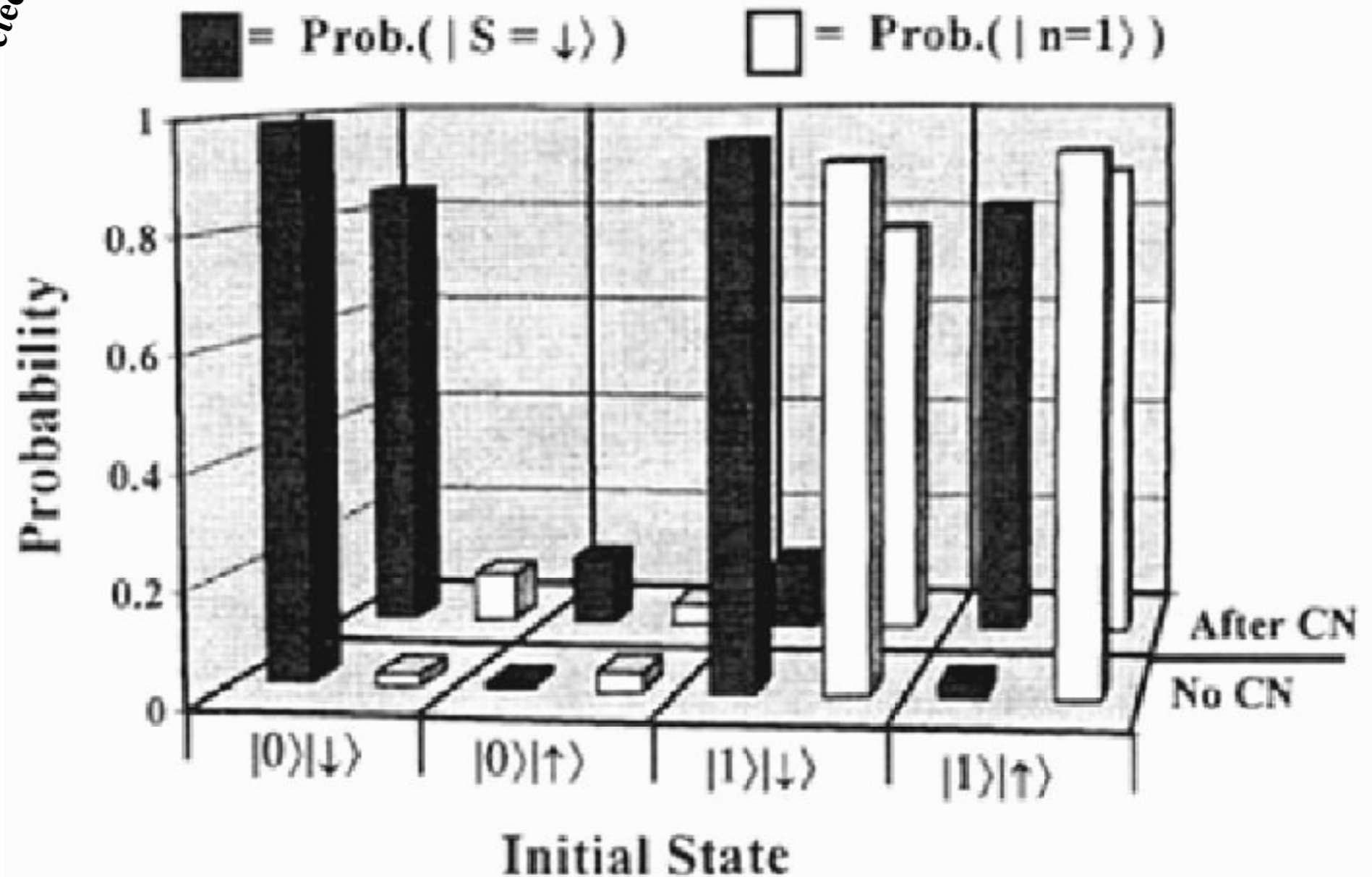
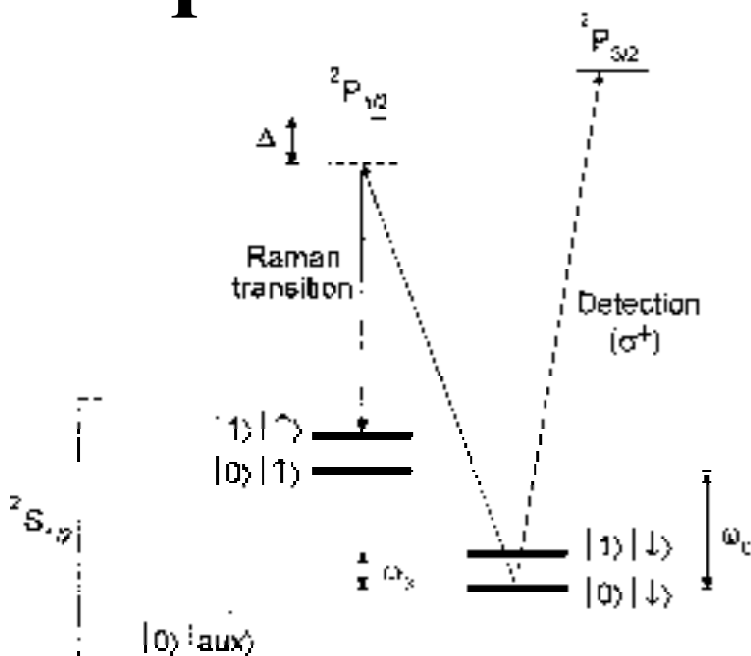
1 qubit

${}^9\text{Be}^+$

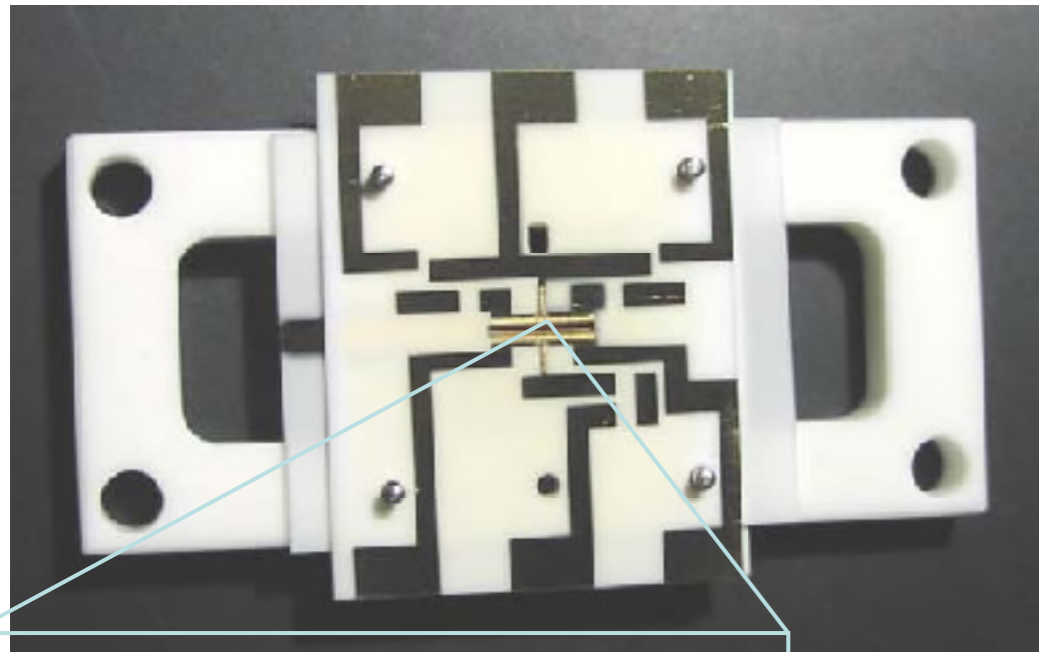


C. Monroe, D.M. Meekhof, B.E. King, W.M. Itano, and D.J. Wineland, 'Demonstration of a fundamental quantum logic gate', Phys. Rev. Lett. 75, 4714 (1995).

2 qubits

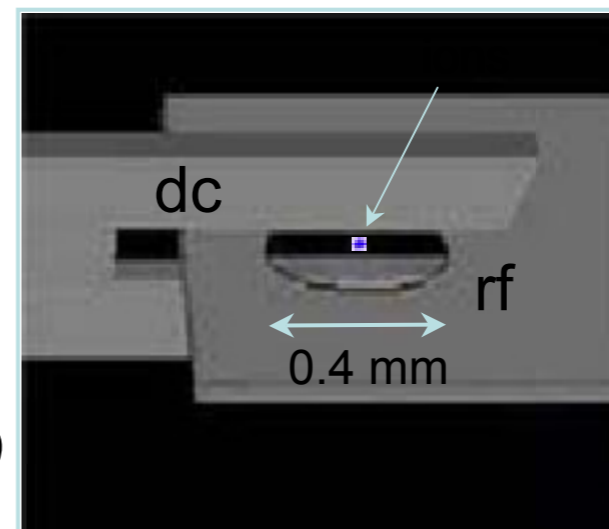
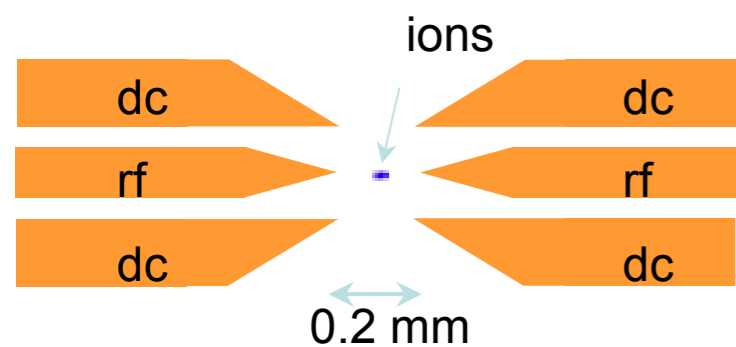


Miniature Traps



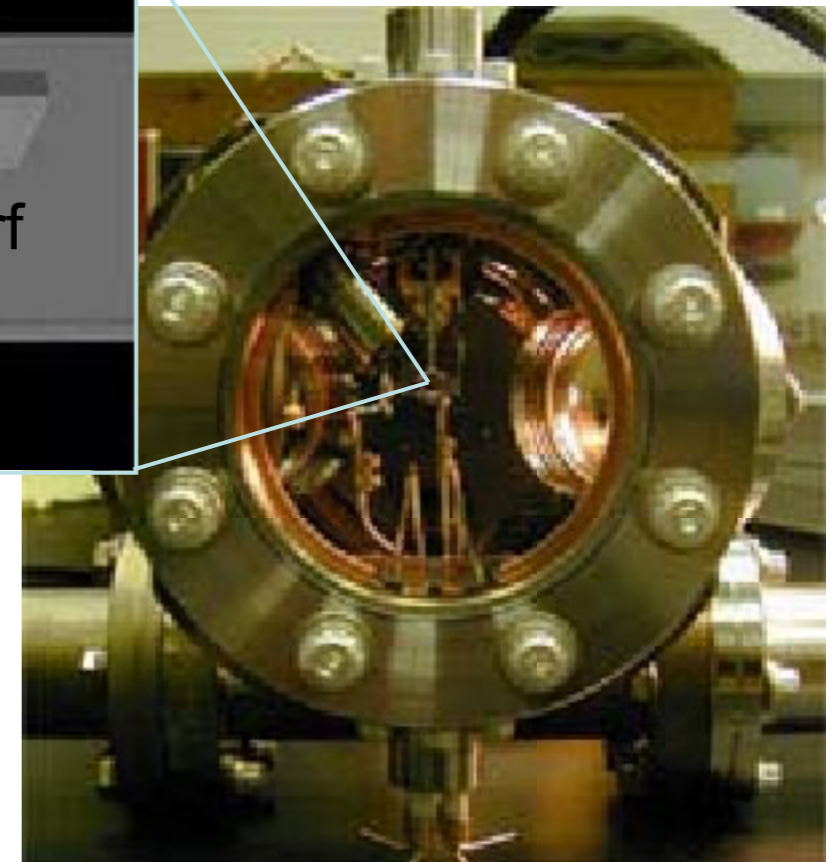
3-layer lithographic linear trap

- RF nodal line (ion string)
- static voltage compensation electrodes
- 200 micron size (strong confinement)



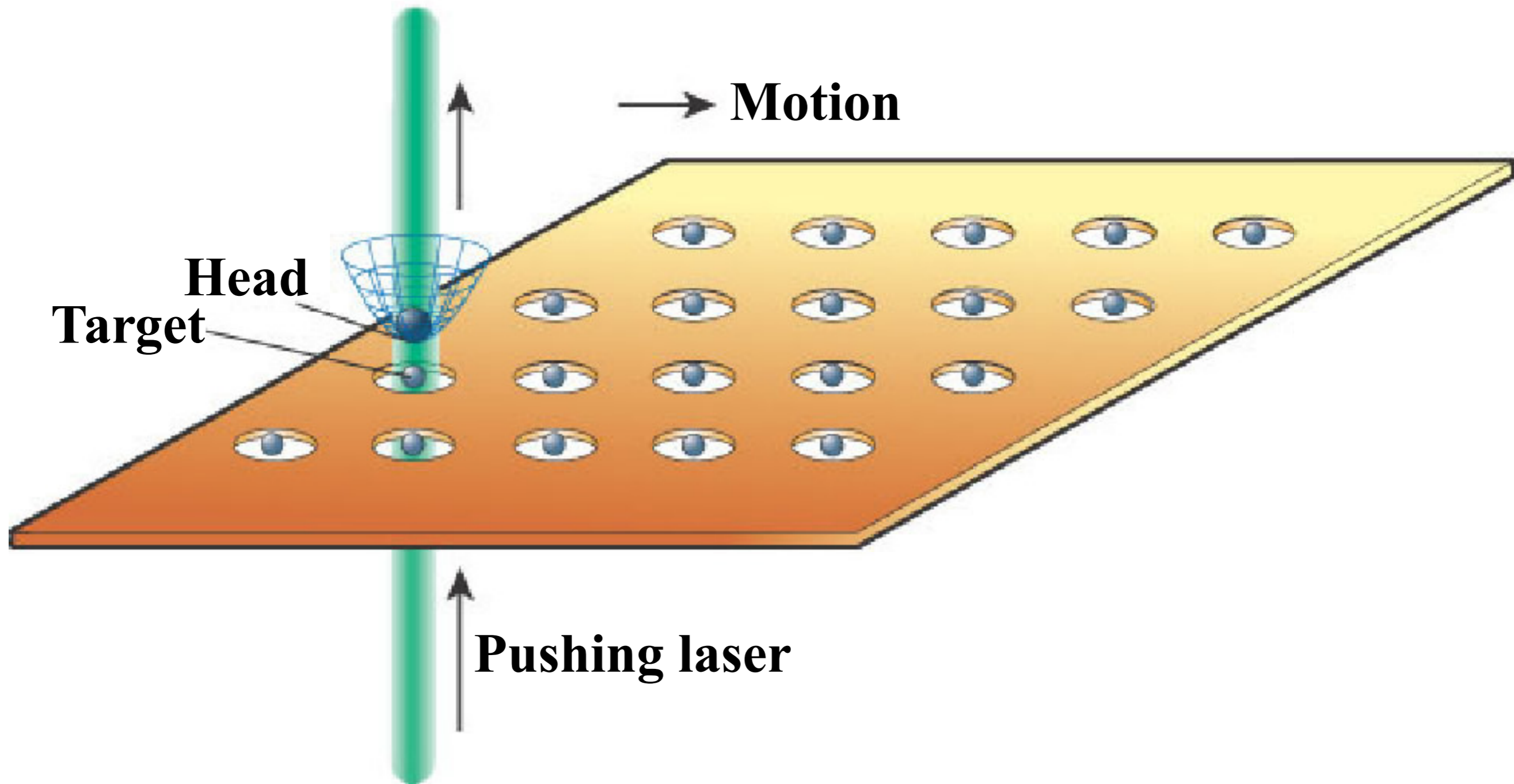
Ring-and-fork quadrupole trap

- easy to build and operate
 - good optical access
- trapping few ions near RF null



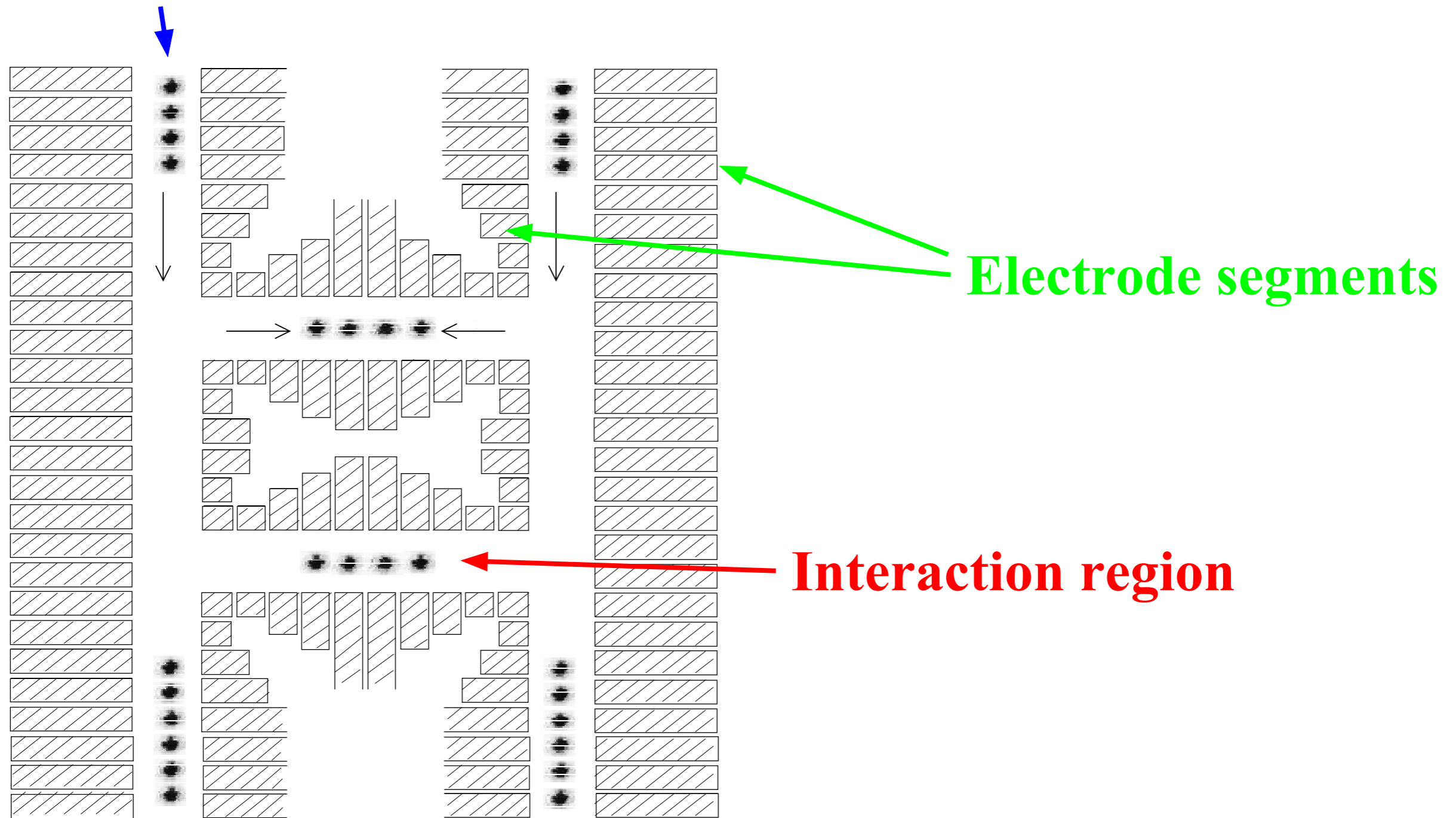
Alternative Traps

J. I. Cirac and P. Zoller, *Nature* 404, 579–581 (2000).



Segmented Traps

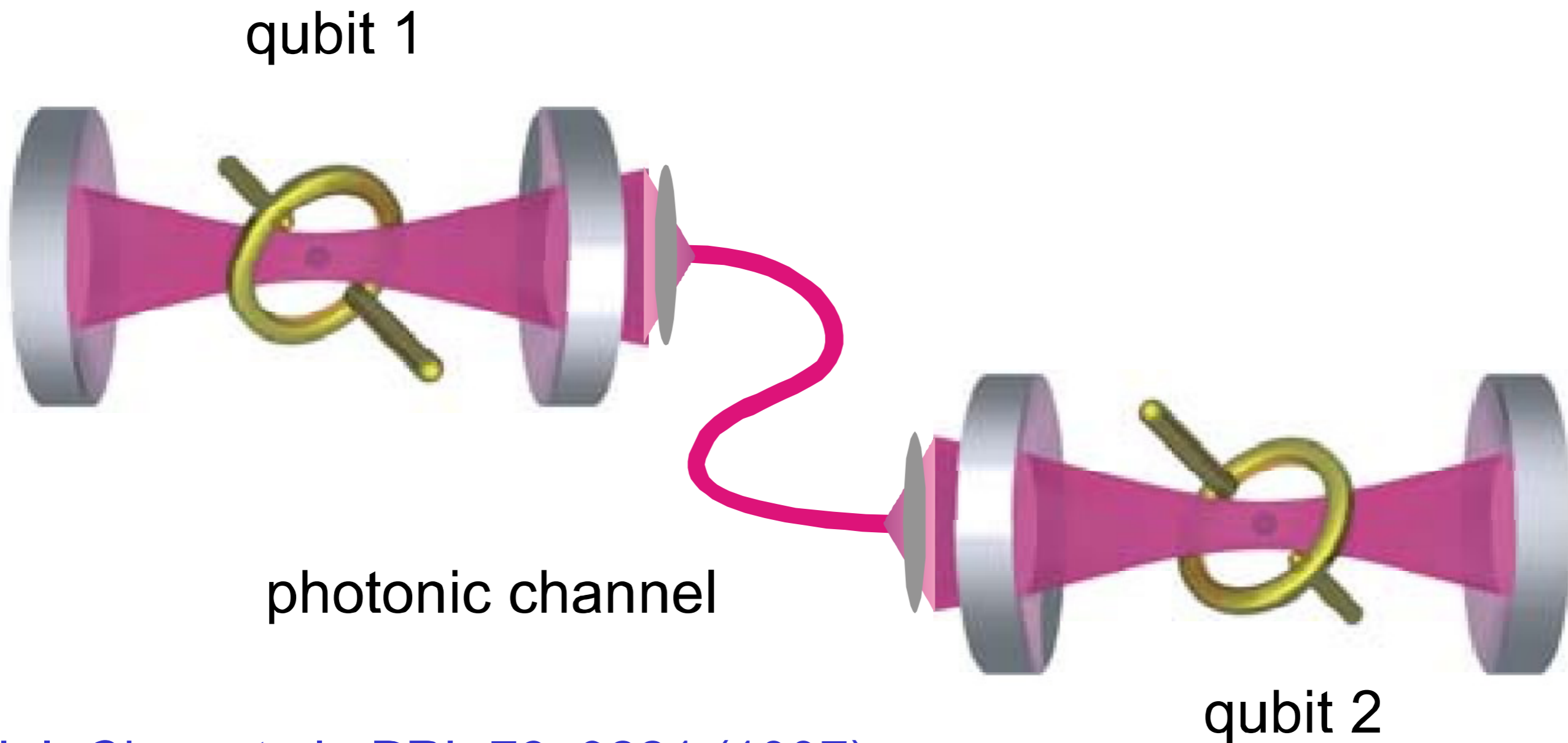
Memory region



D. Kielpinski, C. Monroe, and D.J. Wineland,

‘Architecture for a large-scale ion-trap quantum computer’, Nature 417, 709 (2002).

Coupled Traps



J. I. Cirac et al., PRL 78, 3221 (1997)